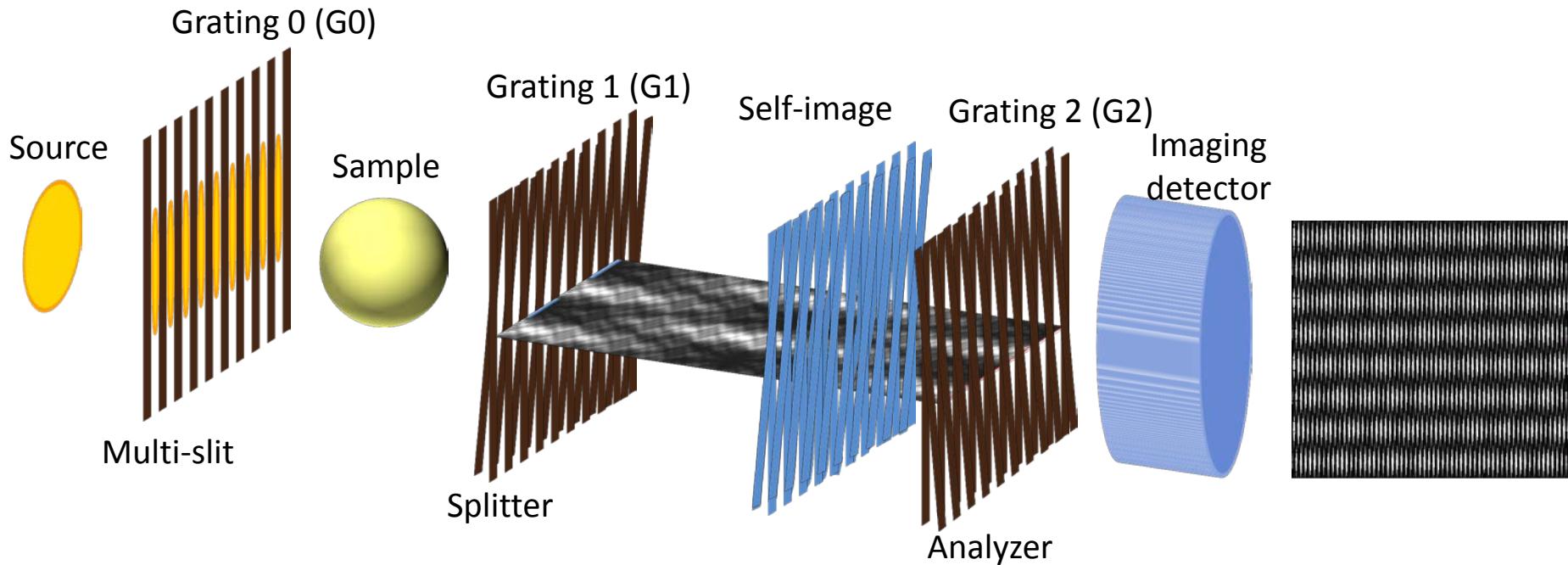


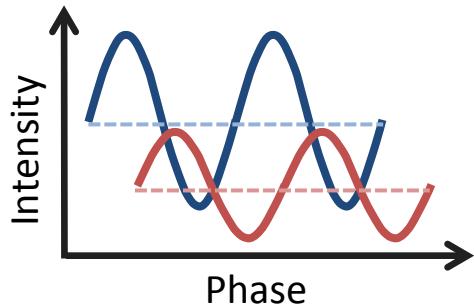
# **J-PARC RADEN における パルス中性子位相イメージングの開発**

**JAEA  
関 義親**

# Talbot-Lau 干渉計の原理



Fresnel回折場→ G2位置にG1直後と同じ強度分布：自己像  
試料による自己像の歪みをG2とのモアレ縞で検出



- 吸収コントラスト像（吸収断面積）
- 微分位相コントラスト像（散乱長）
- ビジビリティコントラスト像（小角散乱）

# 測定される物理量

## 微分位相イメージング

Phase of moiré fringe       $\varphi(x, y) \propto \lambda^2 \frac{\partial}{\partial x} \int b(x, y) \rho(x, y) dz$

## ビジビリティイメージング

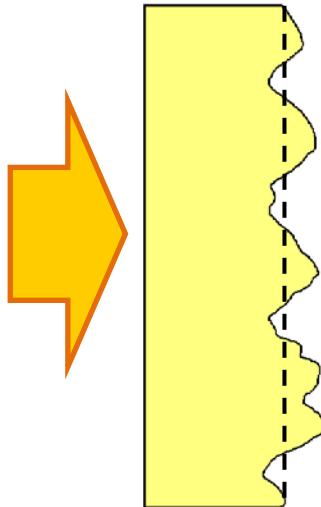
Damping factor of visibility       $\eta \simeq \exp[-\sigma_\Phi^2(x, y)\{1 - \gamma(x, y; -pd_1)\}]$

## Autocorrelation function

$$\gamma(x, y; \Delta x) \simeq \exp \left[ - \left\{ \frac{|\Delta x|}{\xi(x, y)} \right\}^{2H} \right]$$

$b$ : Scattering length,  $\rho$ : Atomic density,  
 $\sigma_\Phi^2$ : Standard deviation of phase,  $\xi$ : Correlation length,  $H$ : Hurst parameter

Neutron beam



$$\Phi(x, y) = \underbrace{\Phi_s(x, y)}_{\text{Phase shift due to averaged structure}} + \underbrace{\Phi_f(x, y)}_{\text{Phase shift due to microstructures}}$$

Phase shift  
due to  
averaged structure

Phase shift  
due to  
microstructures

# J-PARC RADEN における Talbot-Lau 干渉法の高度化

- パルスビームでのTOF測定による  
**波長分解型**Talbot-Lau干渉法

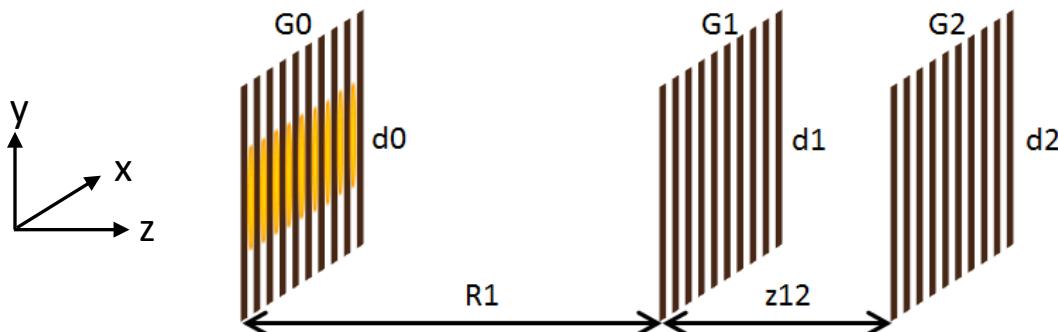
広波長域利用・高波長分解能の両立 → 高精度位相測定  
波長依存性を活かした解析

- 偏極中性子利用による  
**磁気有感型**Talbot-Lau干渉法

磁場勾配測定

磁場構造

# 格子のアライメント条件



$d_0, d_1, d_2$ : Grating pitches  
 $R_1$ : Distance G0-G1  
 $Z_{12}$ : Distance G1-G2  
 $\lambda$ : Wavelength  
 $p$ : Talbot order

- Talbot condition:

Put G2 on the self-image position.

$$z_{12} = p \frac{d_1^2}{\lambda} M$$

$$\begin{cases} p = 1 & (\text{G1: Absorption grating}) \\ 1/2 & (\text{G1: } \pi/2 \text{ phase grating}) \\ 1/8 & (\text{G1: } \pi \text{ phase grating}) \end{cases}$$

- Lau condition:

Superpose self-images from each line source of G0 constructively.

$$\frac{d_0}{d_2} = \frac{R_1}{z_{12}}$$

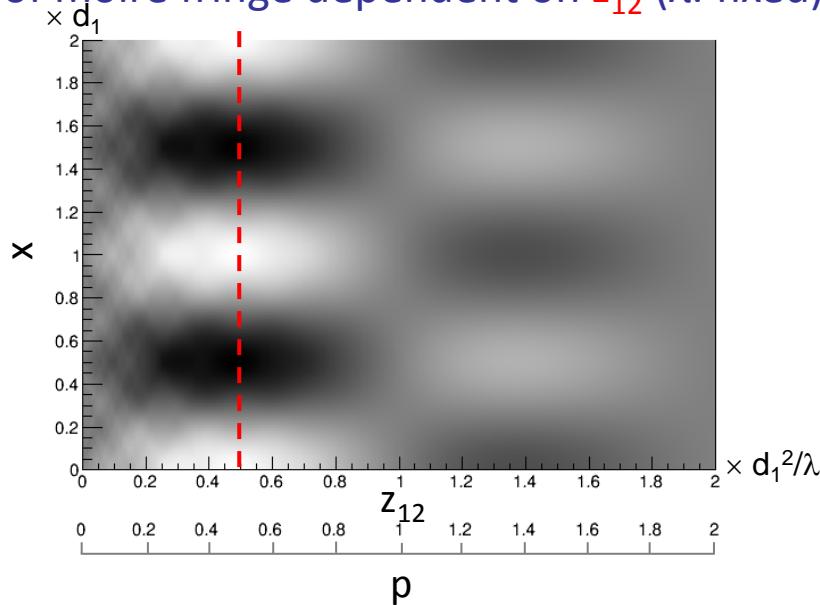
- Magnification due to spherical wave propagation

$$d_2 = d_1 M$$

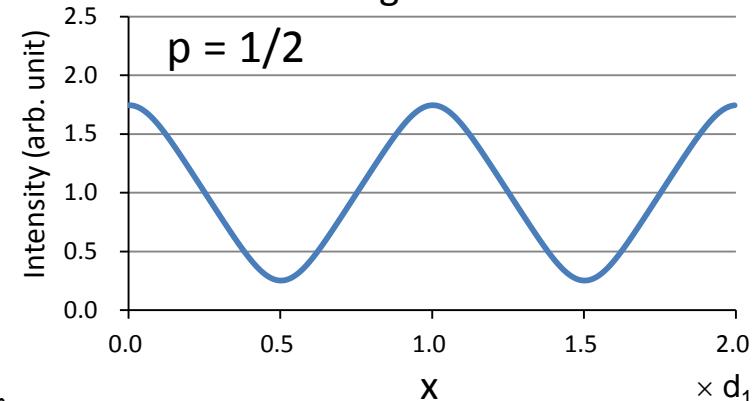
$$M = \frac{R_1 + z_{12}}{R_1}$$

# 低ビームコヒーレンス下でのモアレ縞

Visibility of moiré fringe dependent on  $z_{12}$  ( $\lambda$ : fixed)

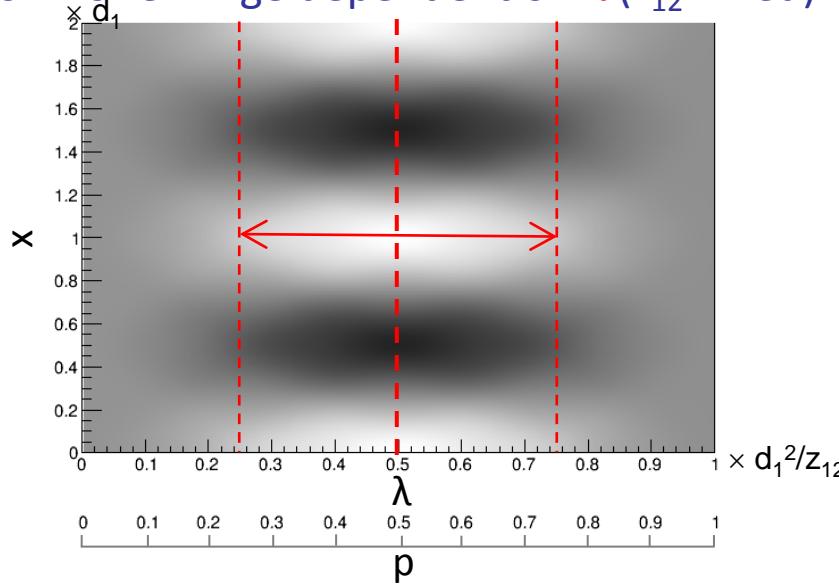


Moiré fringe between self-image of G1 and G2



Moiré fringes are observable around  $z_{12} = 0.5 \times d_{12}/\lambda$  ( $p = 1/2$ ).

Visibility of moiré fringe dependent on  $\lambda$  ( $z_{12}$ : fixed)



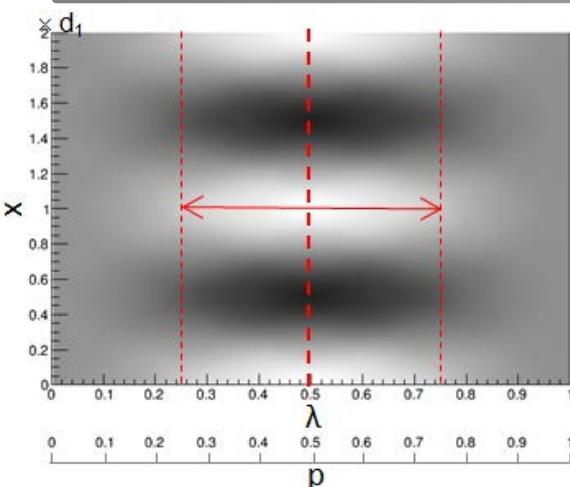
$$z_{12} = p \frac{d_1^2}{\lambda}$$

$$z_{12}\lambda \propto p$$

Moiré fringes are observable around  $\lambda = 0.5 \times d_{12}/z_{12}$  ( $p = 1/2$ ).

$$\Delta\lambda/\lambda \sim 50\%$$

# Advantages of wavelength-resolved TL interferometry



Phase determination precision  
for moiré fringe

$$\Delta\psi \propto \frac{1}{\sqrt{NV}}$$

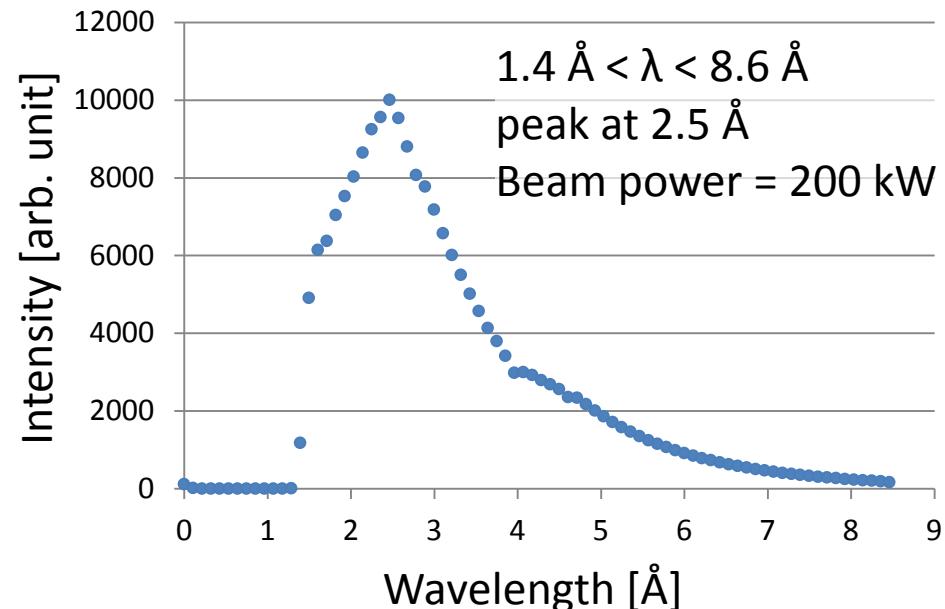
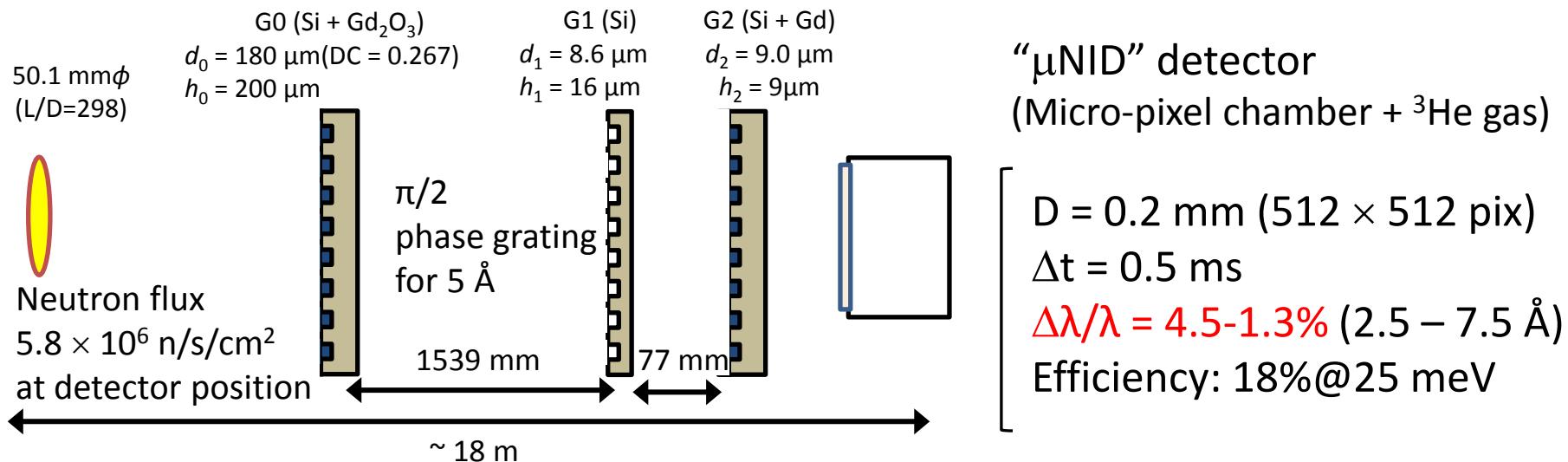
Chromatic aberration  
of moiré phase

$$\Delta\psi_{c.a.}/\psi = 2\Delta\lambda/\lambda$$

N: Statistics  
V: Moiré visibility  
 $\Delta\lambda$ : Band width

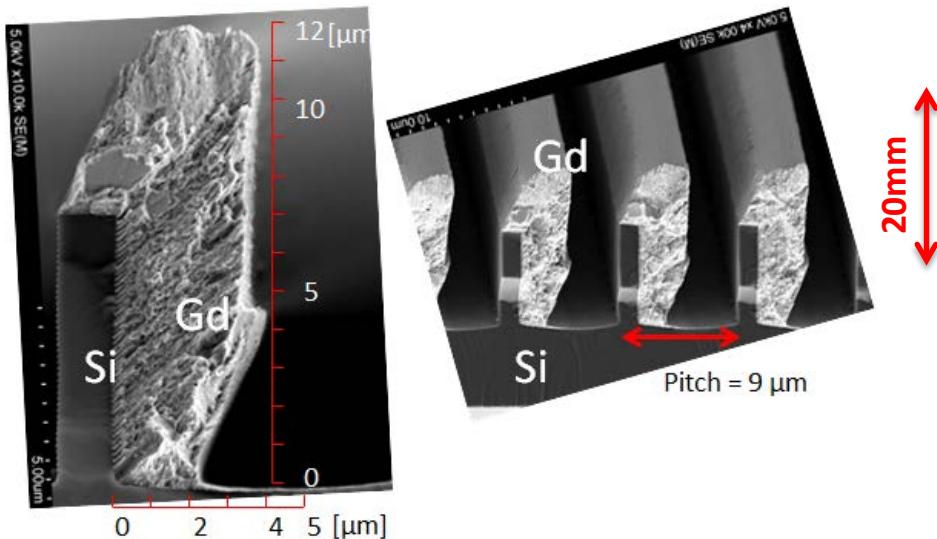
- Wide wavelength band with fine wavelength resolution
  - Wide band → High statistics
  - Fine resolution → avoid chromatic aberration → High visibility→ Increase phase precision and accuracy
- Wavelength dependence of physical quantity
  - Differential phase contrast imaging  $\propto \lambda^2$
  - Visibility contrast imagingAutocorrelation function with different scales

# Experiment at RADEN in J-PARC

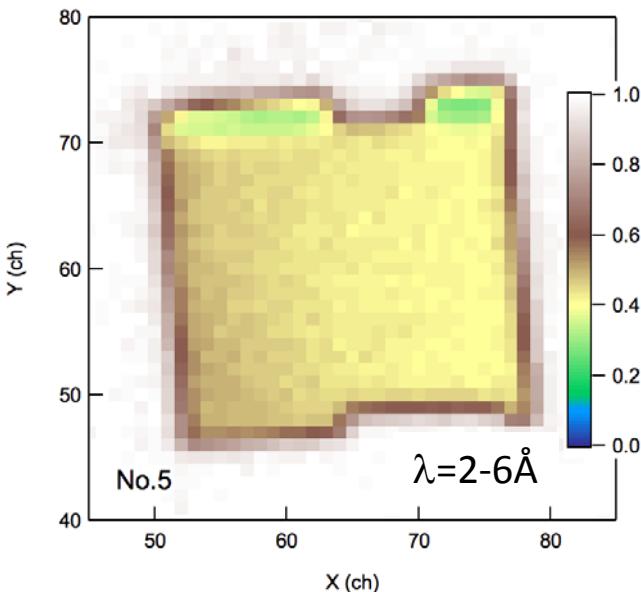


# Fabrication of absorption grating with fine pitch (G2)

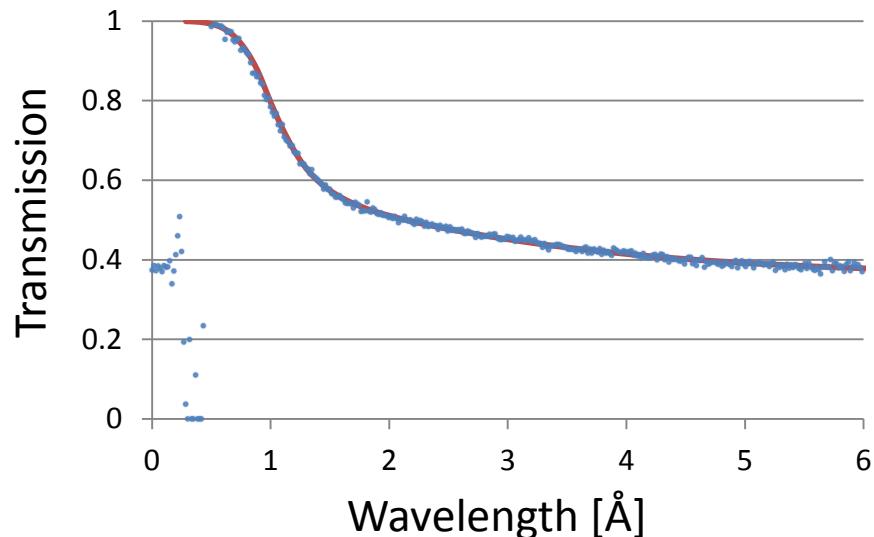
## Gd evaporation method



Neutron transmission image



Wavelength dependence of neutron transmission



Effective Gd thickness 9.0  $\mu\text{m}$   
Duty cycle 0.36

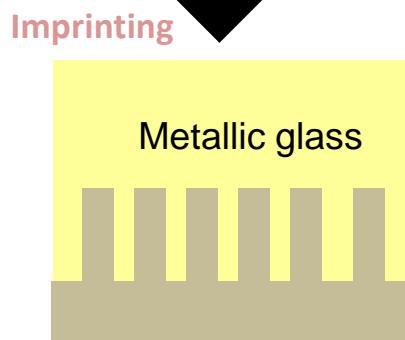
On the assumption of  
ideal shape of Ronchi grating

# Fabrication of Absorption Grating

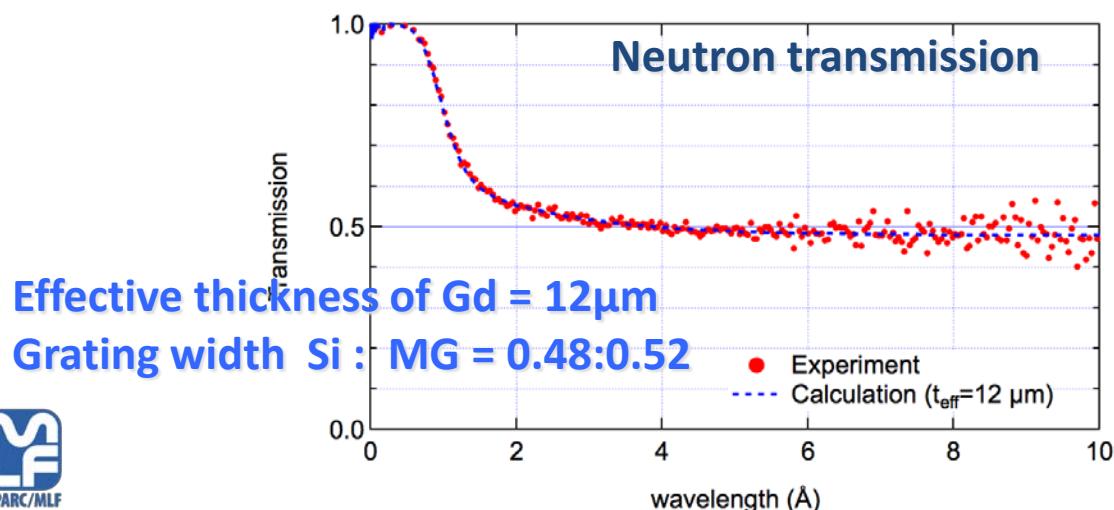
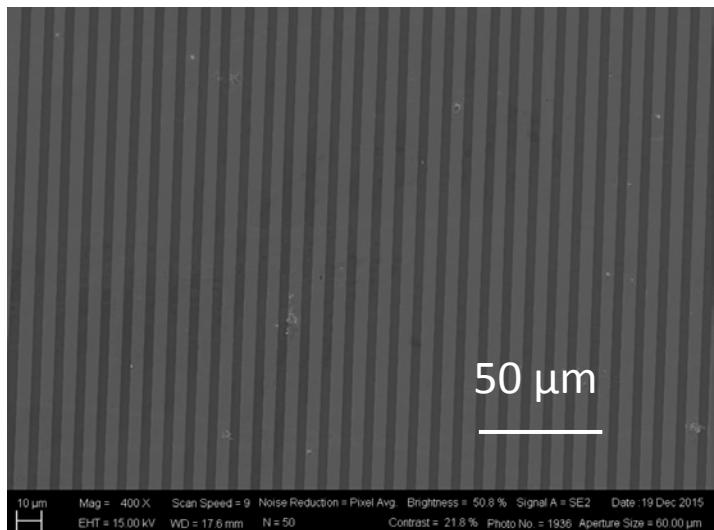
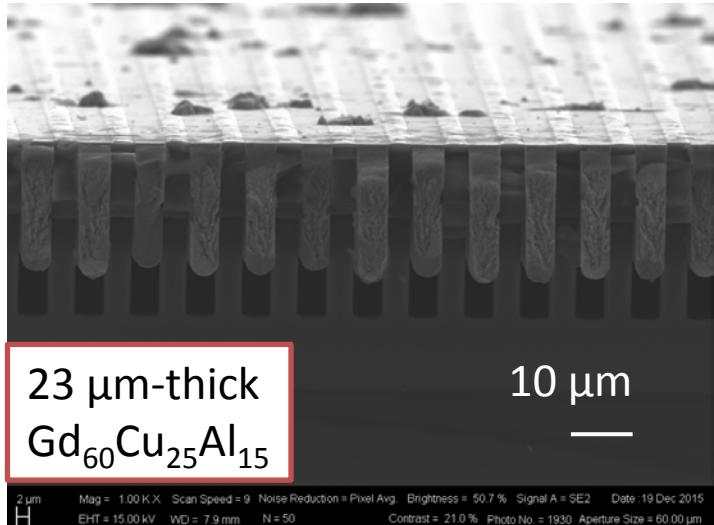


## Gd based metallic glass imprinting

W. Yashiro et al., APEX, 7 (2014) 032501.  
W. Yashiro et al., JJAP, 55 (2016) 048003.

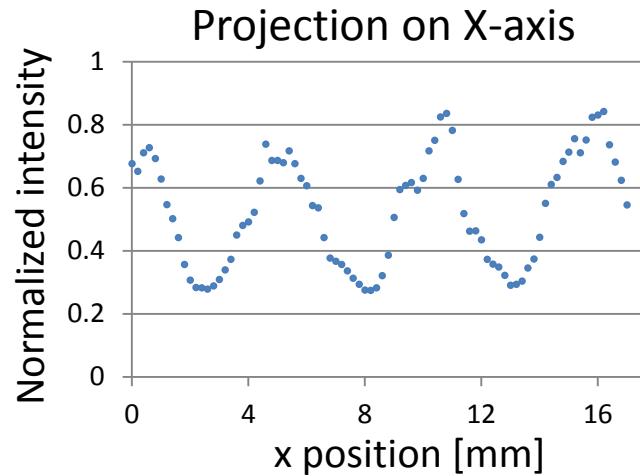
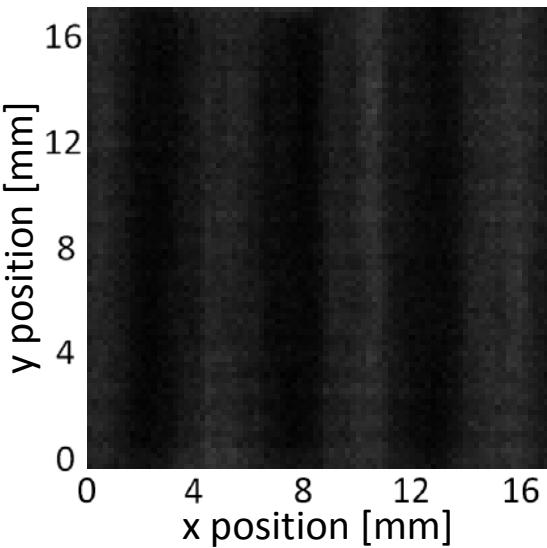


Etching extra glass  
by ion beam  
milling process



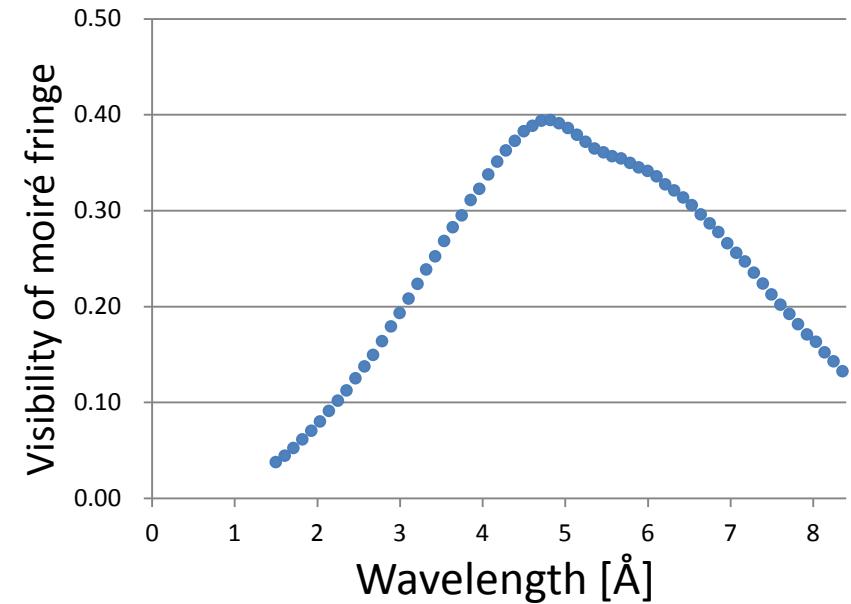
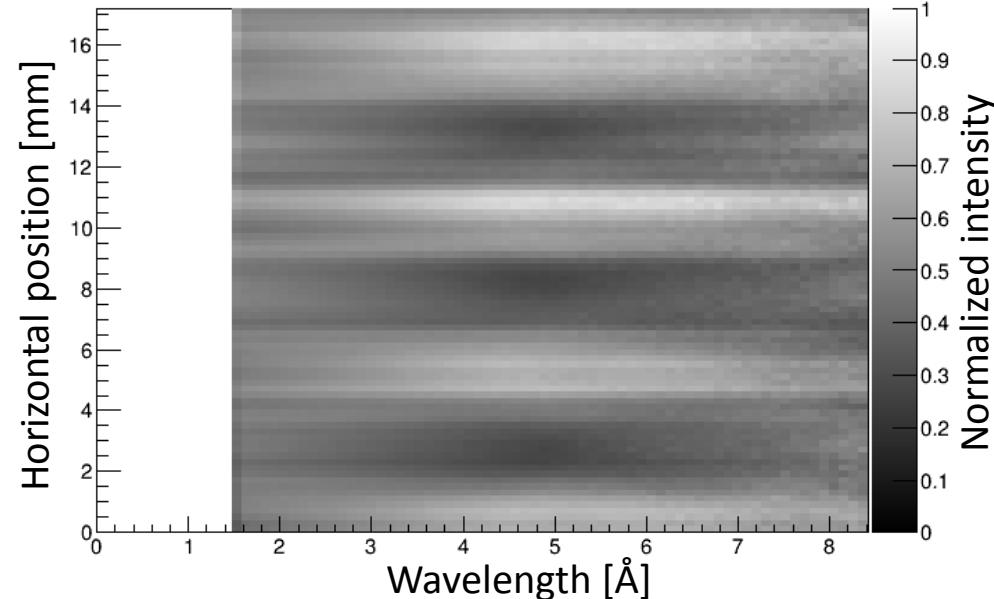
# Observation of moiré fringe (without sample)

Moiré fringe (at  $\lambda = 5.0 \text{ \AA}$ )



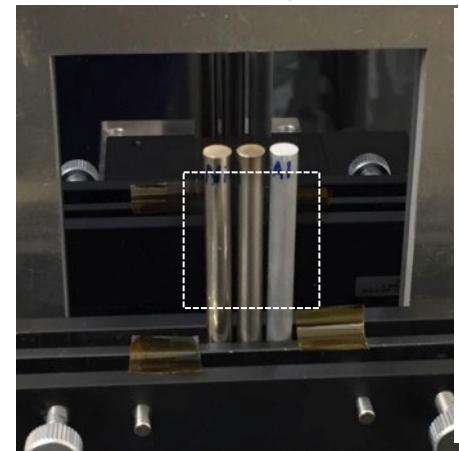
Fringe pattern  
can be seen over  
full wavelength range.

Wavelength dependence of moiré fringe (projected)

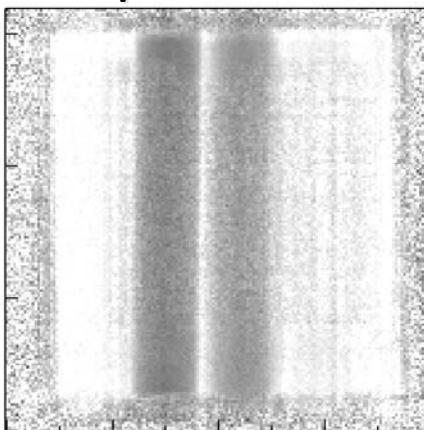


# Phase imaging with TOF method

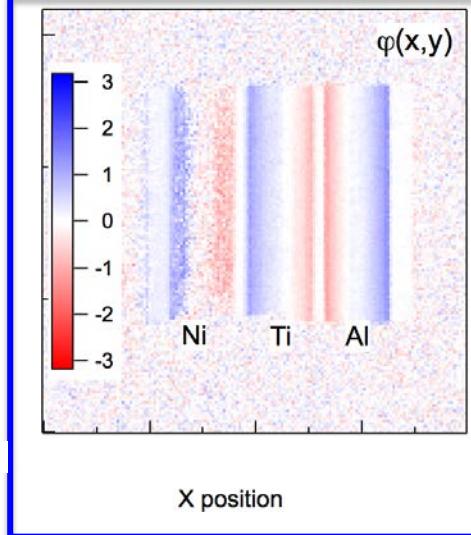
Ni, Ti, Al rods ( $\phi=5\text{mm}$ )



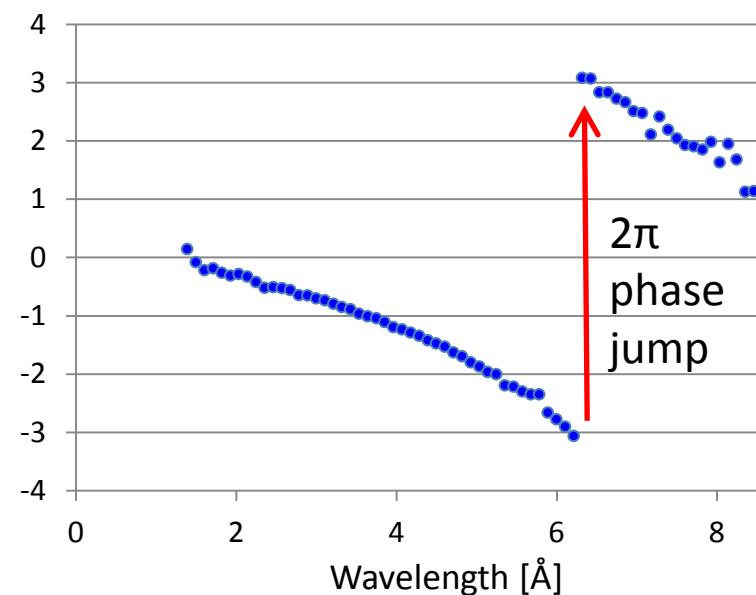
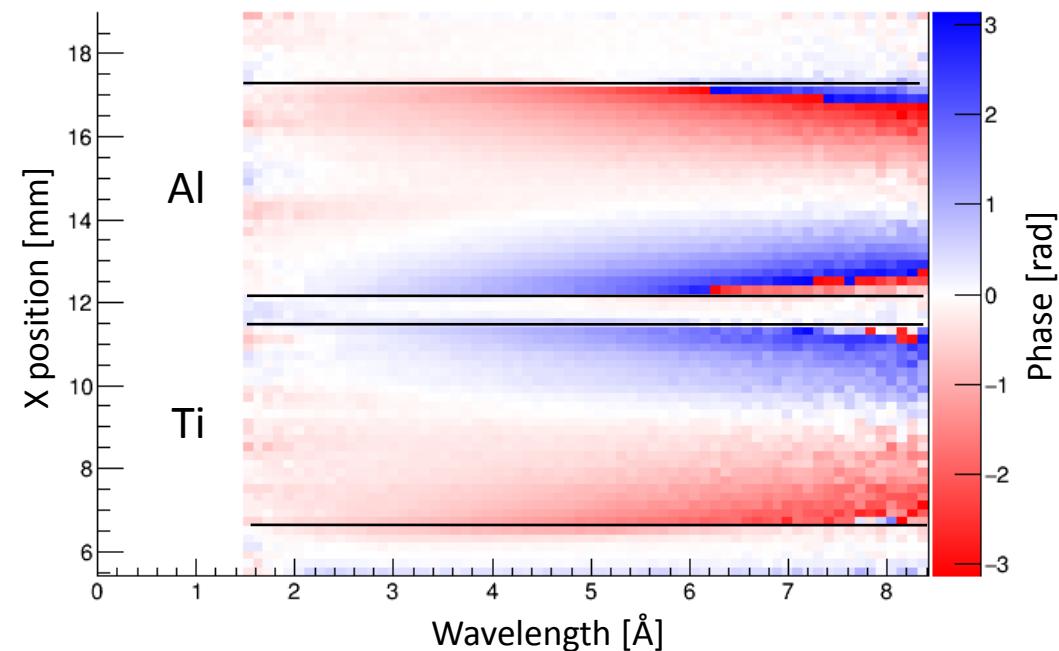
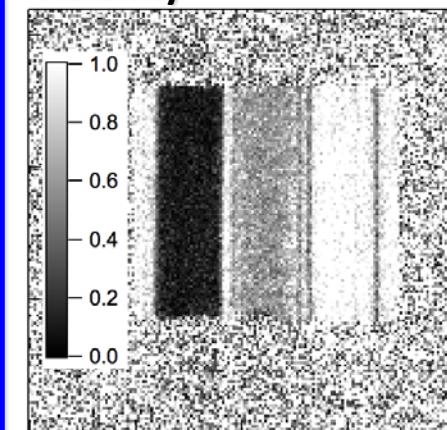
Absorption



Differential Phase



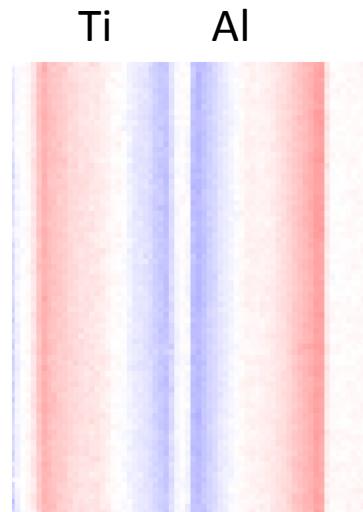
Visibility



# Wide wavelength band vs narrow wavelength band

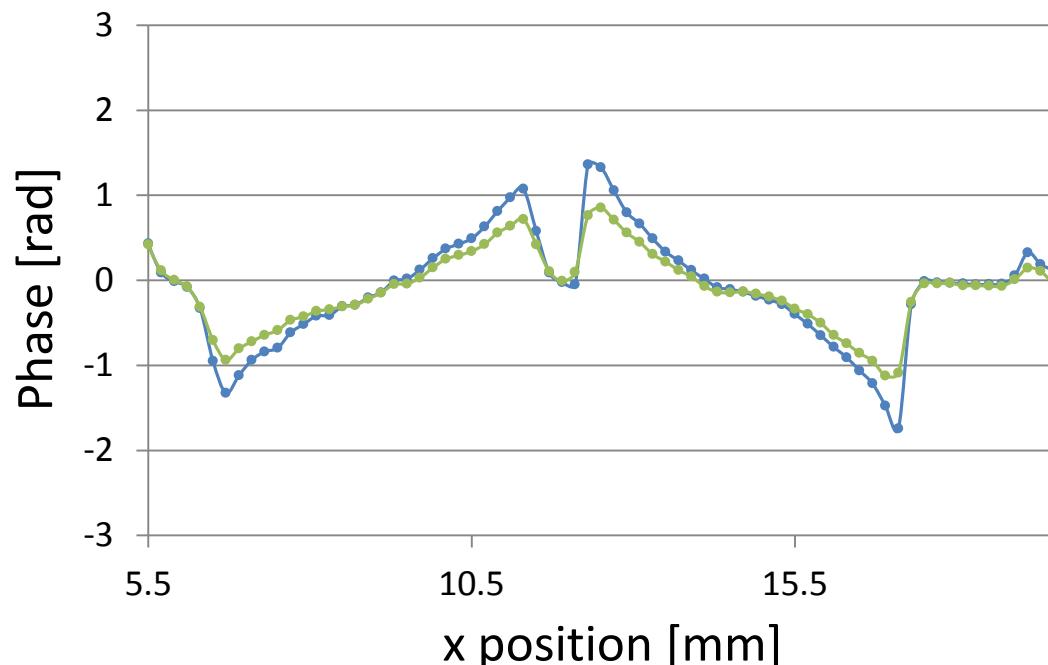
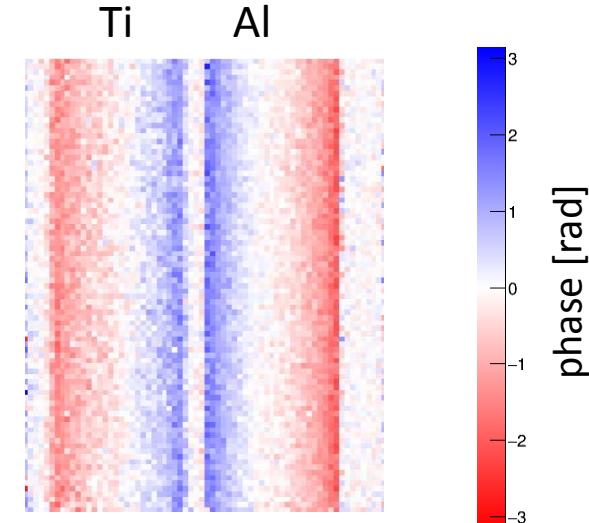
$\lambda = 5 \text{ \AA}$  (2.5-7.5 \AA)  
 $\Delta\lambda/\lambda = 50\%$

High statistics,  
but low contrast.



$\lambda = 5 \text{ \AA}$   
 $\Delta\lambda/\lambda = 2\%$

High contrast,  
but noisy.

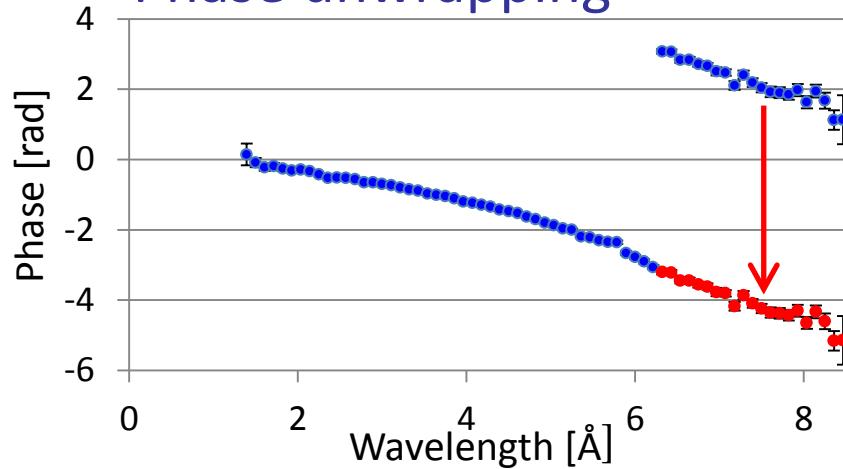


- $\Delta\lambda/\lambda = 50\%$   
Stat. error  $4 \times 10^{-3} \text{ rad}$
- $\Delta\lambda/\lambda = 2\%$   
Stat. error  $3 \times 10^{-2} \text{ rad}$

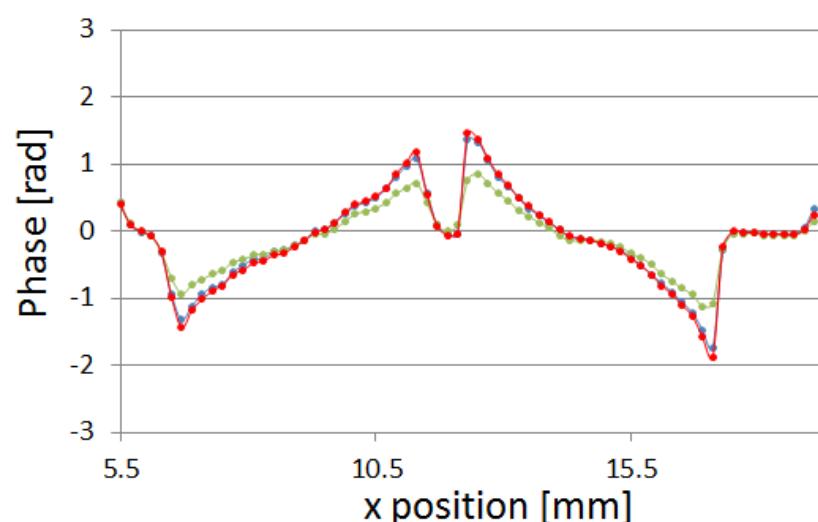
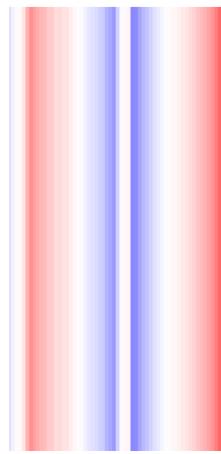
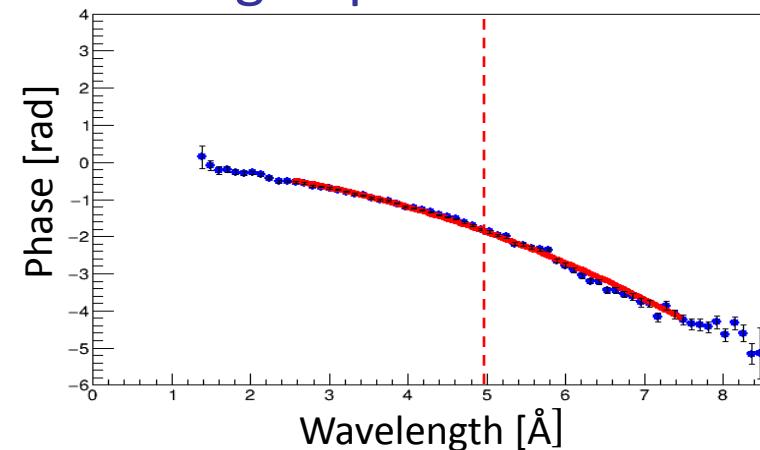
# Wide wavelength band + TOF

Phase  $\propto \lambda^2$

Phase unwrapping



Fitting to parabola



High statistics,  
and high contrast.

- $\Delta\lambda/\lambda = 50\%$   
Stat. error  $4 \times 10^{-3}$  rad
- $\Delta\lambda/\lambda = 2\%$   
Stat. error  $3 \times 10^{-2}$  rad
- $\Delta\lambda/\lambda = 50\% + \text{TOF}$   
Stat. error  $4 \times 10^{-3}$  rad

# Summary

---

- Pulsed Talbot-Lau interferometry with TOF method at RADN, J-PARC.
- Differential phase contrast imaging with wide wavelength band (50%) and fine wavelength resolution ( $\sim 3\%$ ).
- Phase analysis method with  $\lambda^2$  dependence increases the dynamic range of phase detection in TL interferometer.
- Fabrication of absorption grating with Gd evaporation and imprinting of metallic glass
- Polarized TL interferometry