

Beam Instrumentation and Diagnostics

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FFA'18 School
KURNS, OSAKA

References, Resources

Books

P. Strehl; *Beam Instrumentation and Diagnostics*, Springer 2006.

M.G. Minty; *Measurement and Control of Charged Particle Beams*, Springer 2003.

A. Chao; *Handbook of Accelerator Physics and Engineering*, World Scientific 2013.

Lectures on Particle Accelerators

CERN Accelerator School (CAS)

<http://cas.web.cern.ch>

Joint Universities Accelerator School (JUAS)

<https://indico.cern.ch/category/3833/>

US Particle Accelerator School (USPAS)

<http://uspas.fnal.gov/index.shtml>

KEK Accelerator Seminar (OHO)

<http://accwww2.kek.jp/oho/index.html>

Typical beam parameters and instruments (1/2)

Beam parameters		Instuments	
		LINAC & transfer line	Synchrotron
Current I	<i>General</i>	Transformer, dc & ac Faraday Cup	Transformer, dc & ac
	<i>Special</i>	Particle Detectors	Pick-up Signal (relative)
Profile x_{width}	<i>General</i>	Screens, SEM-Grids Wire Scanners, OTR Screen	Residual Gas Monitor Wire Scanner, Synchrotron Light Monitor
	<i>Special</i>	MWPC, Fluorescence Light	
Position x_{cm}	<i>General</i>	Pick-up	Pick-up
	<i>Special</i>	Using position measurement	
Transverse Emittance ϵ_{trans}	<i>General</i>	Slit-grid Quadrupole Variation	Residual Gas Monitor Wire Scanner
	<i>Special</i>	Pepper-Pot	Transverse Schottky

Typical beam parameters and Instruments (2/2)

Beam parameters		Instruments	
		LINAC & transfer line	Synchrotron
Bunch Length $\Delta\phi$	<i>General</i>	Pick-up	Pick-up Wall Current Monitor
	<i>Special</i>	Secondary electrons	Streak Camera Electro-optical laser mod.
Momentum p and Momentum Spread $\Delta p/p$	<i>General</i>	Pick-up (Time-of-Flight)	Pick-up (e.g. tomography)
	<i>Special</i>	Magnetic Spectrometer	Schottky Noise Spectrum
Longitudinal Emittance ϵ_{long}	<i>General</i>	Buncher variation	Pick-up & tomography
	<i>Special</i>	Magnetic Spectrometer	
Tune and Chromaticity Q, ξ	<i>General</i>	---	Exciter + Pick-up Transverse Schottky Spectrum
	<i>Special</i>	---	
Beam Loss r_{loss}	<i>General</i>	Particle Detectors (Ionization chambers, PIN diodes, Optical fibers)	
Polarization P	<i>General</i>	Particle Detectors	
	<i>Special</i>	Laser Scattering (Compton scattering)	
Luminosity L	<i>General</i>	Particle Detectors	

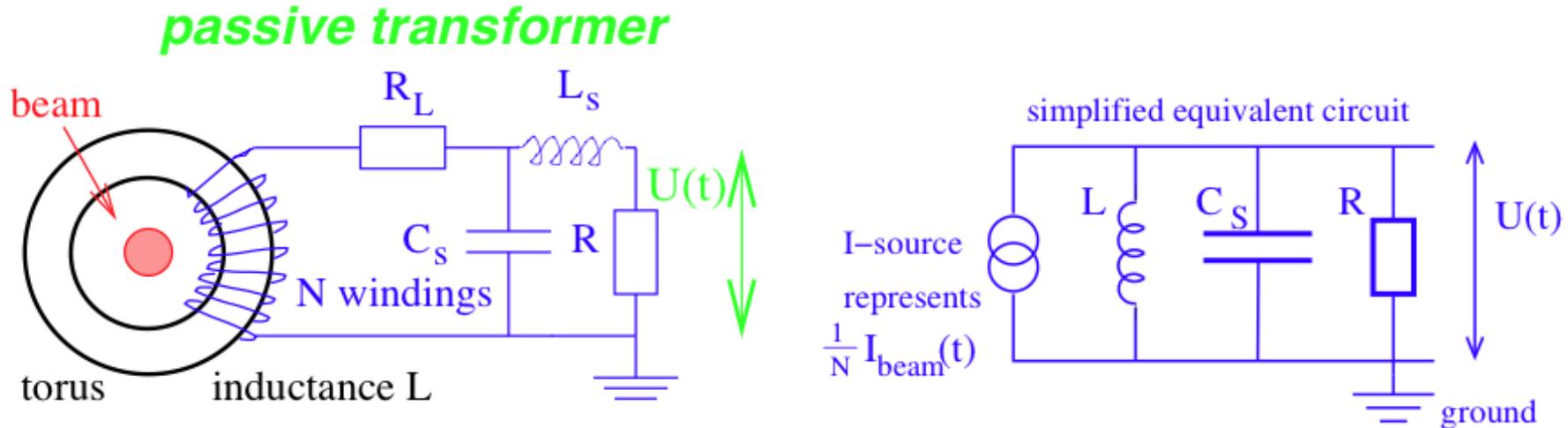
P.Forck CAS2013

- **Destructive** and **non-destructive** devices depending on the beam parameters
- Different techniques for the same parameters <--> Same techniques for the different parameters

Beam intensity monitor

Passive Transformer (Fast Current Transformer : FCT)

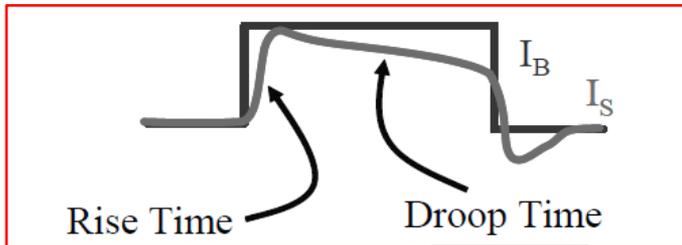
Simplified electrical circuit of a passively loaded transformer:



H.Koziol CAS

A voltages is measured: $U = R \cdot I_{sec} = R / N \cdot I_{beam} \equiv S \cdot I_{beam}$

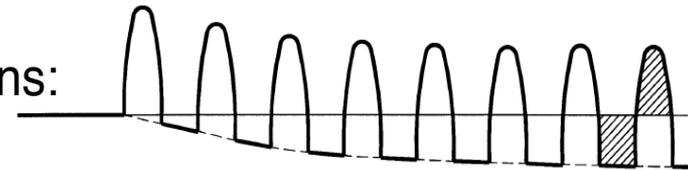
with **S sensitivity** [V/A], equivalent to transfer function or transfer impedance **Z**



$$\tau_{rise} = \sqrt{L_s C_s}$$

$$\tau_{droop} = L / (R + R_L)$$

Bunch trains:



- Equal areas
- Baseline shift proportional to intensity

Active Transformer with long droop time

Active Transformer or Alternating Current Transformer ACT:

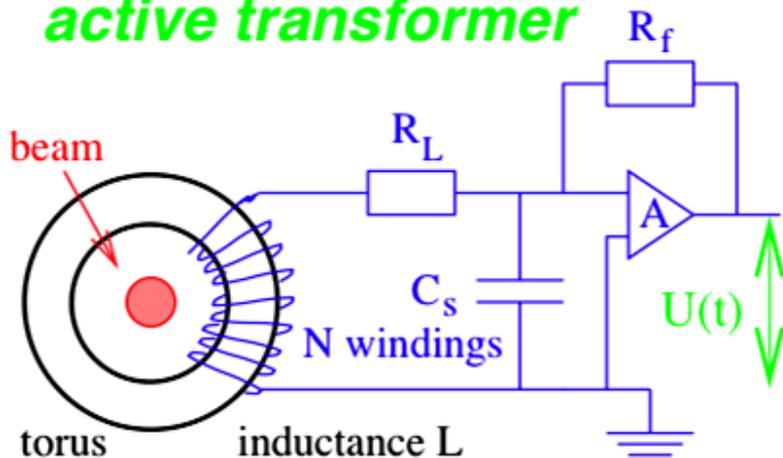
uses a trans-impedance amplifier (I/U converter) to $R \approx 0 \Omega$ load impedance i.e. a current sink

+ compensation feedback

\Rightarrow longer droop time τ_{droop} and rise time τ_{rise}

Application: measurement of longer $t > 10 \mu s$ e.g. at pulsed LINACs

active transformer



The input resistor is for an op-amp: $R_f/A \ll R_L$

$$\Rightarrow \tau_{droop} = L/(R_f/A + R_L) \approx L/R_L$$

Droop time constant can be up to 1 s!

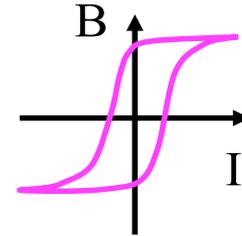
The feedback resistor is also used for range switching.

An additional active feedback loop is used to compensate the droop.

DC beam Current Transformers (DCCT)

K.Uncser(CERN1969)~

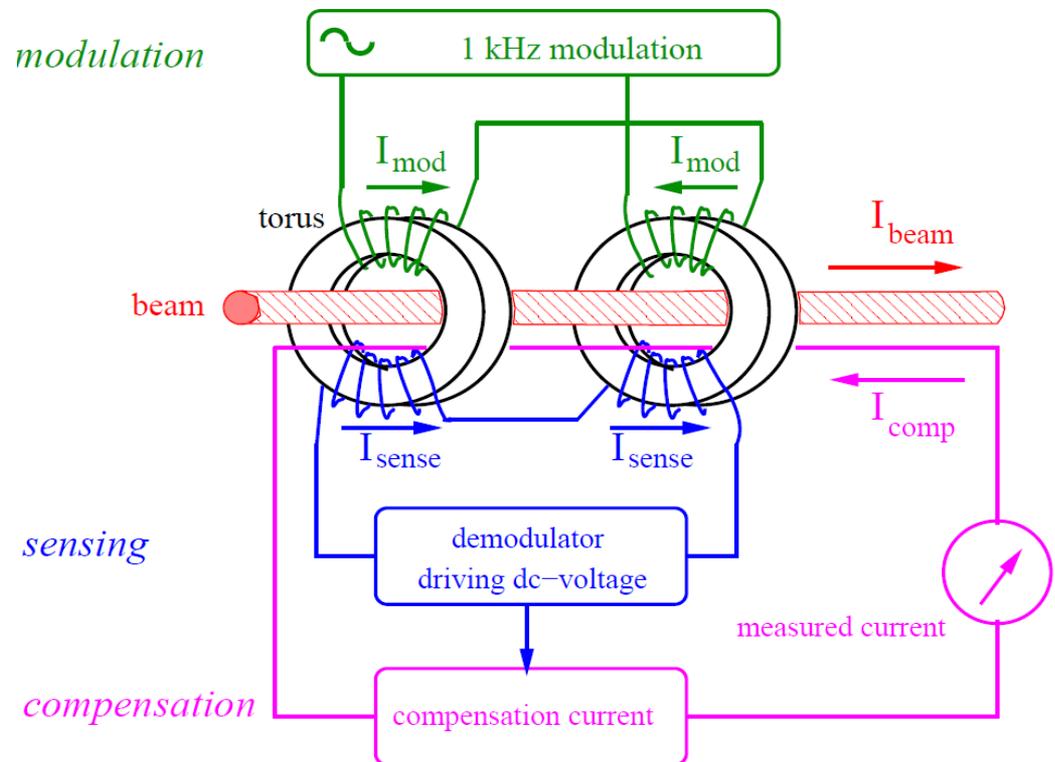
- DC current $dB/dt = 0 \Rightarrow$ no voltage induced
- Use two **identical** toroids
- Take advantage of non-linear magnetisation curve



- **Modulation** of opposite sign drives toroids into saturation
- **Sense windings** measure the modulation signal
 - Signals from the two toroids cancel each other out as long as there is no beam

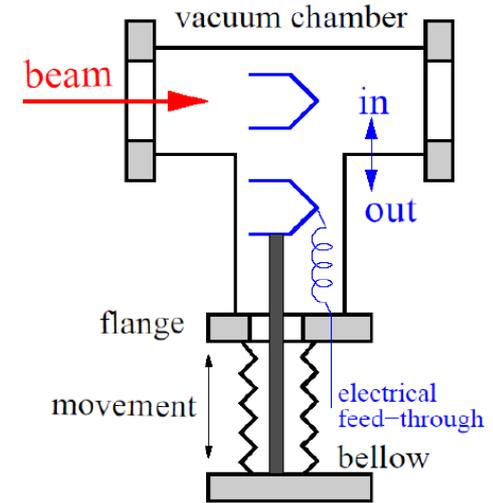
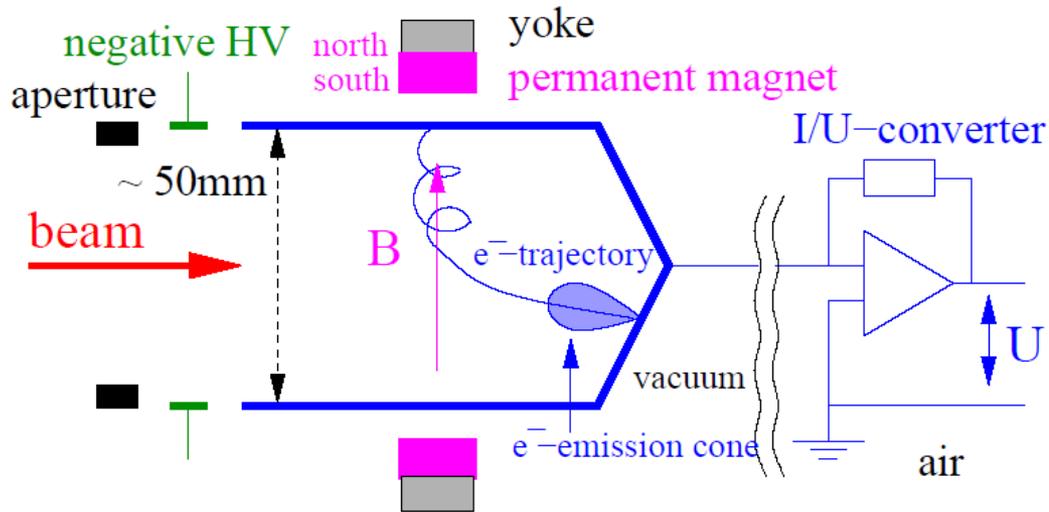
➤ But with the I_{beam} , the saturation is shifted and I_{sense} is not zero

➤ **Compensation current** adjustable until I_{sense} is zero once again



Faraday Cups

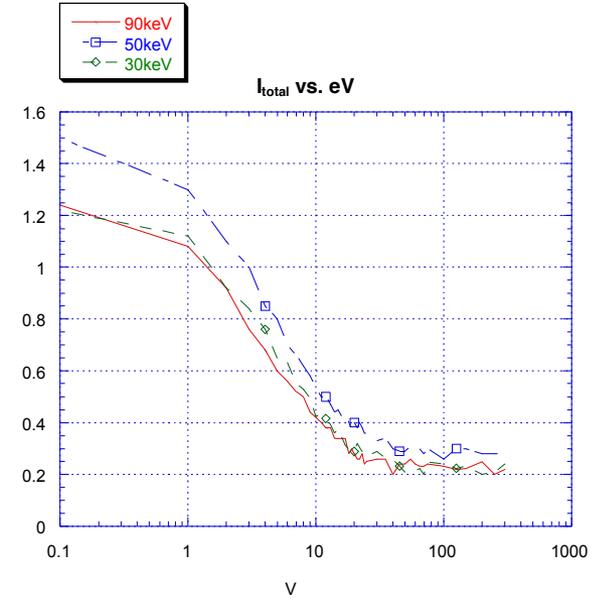
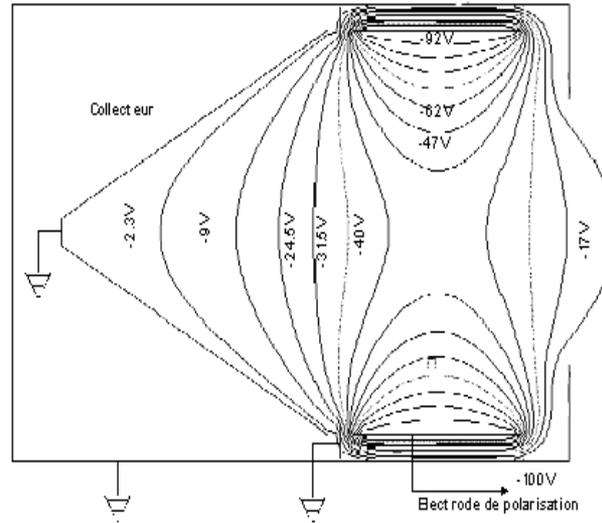
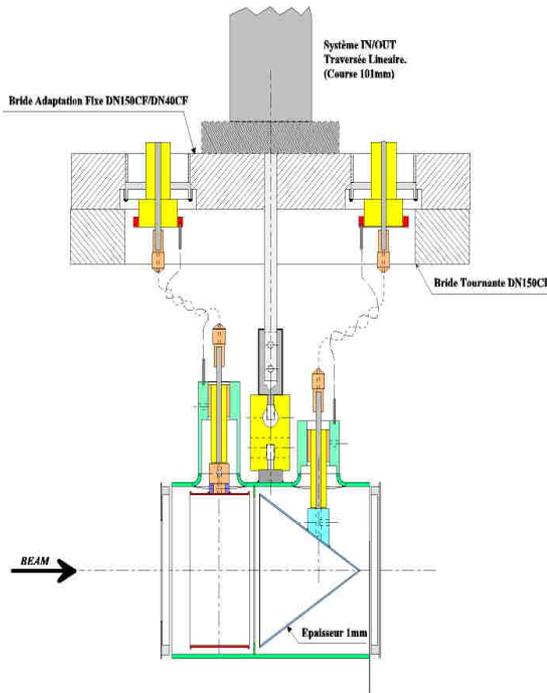
The beam particles are collected inside a metal cup
The beam's charge are recorded as a function of time.



GSI Faraday cup

Currents down to 10 pA with bandwidth of 100 Hz!
To prevent for secondary electrons leaving the cup
Magnetic field and/or **Electric field**
for potential barrier at the cup entrance

Faraday Cups : repelling voltage



In order to keep secondary electrons with the cup a repelling voltage is applied to the polarization electrode

Since the electrons have energies of less than 20 eV some 100V repelling voltage is sufficient

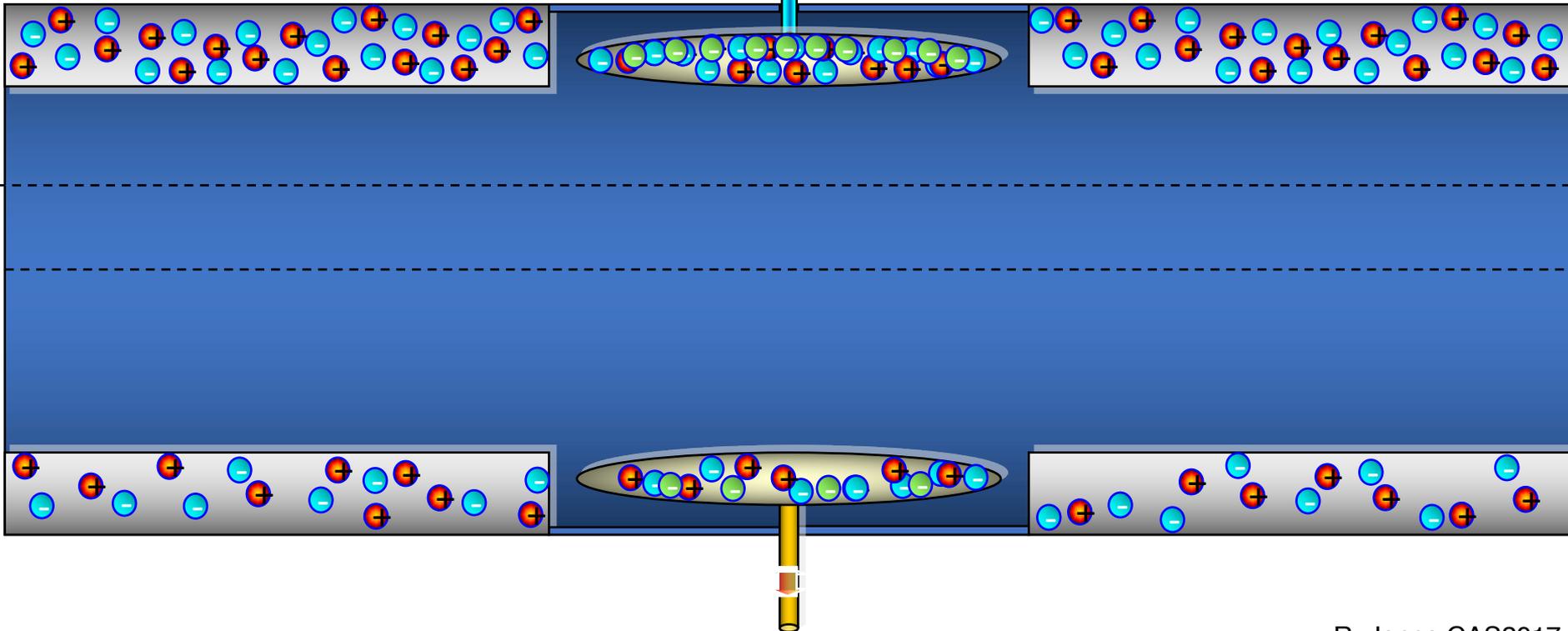
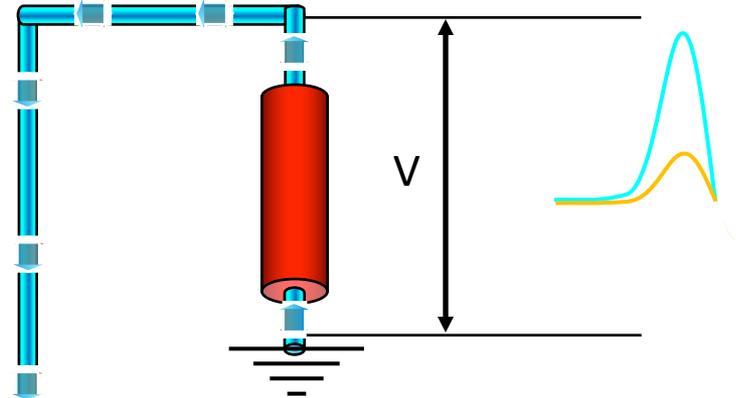
With increasing repelling voltage the electrons do not escape the Faraday Cup any more and the current measured stays stable.

At 40V and above no decrease in the Cup current is observed any more

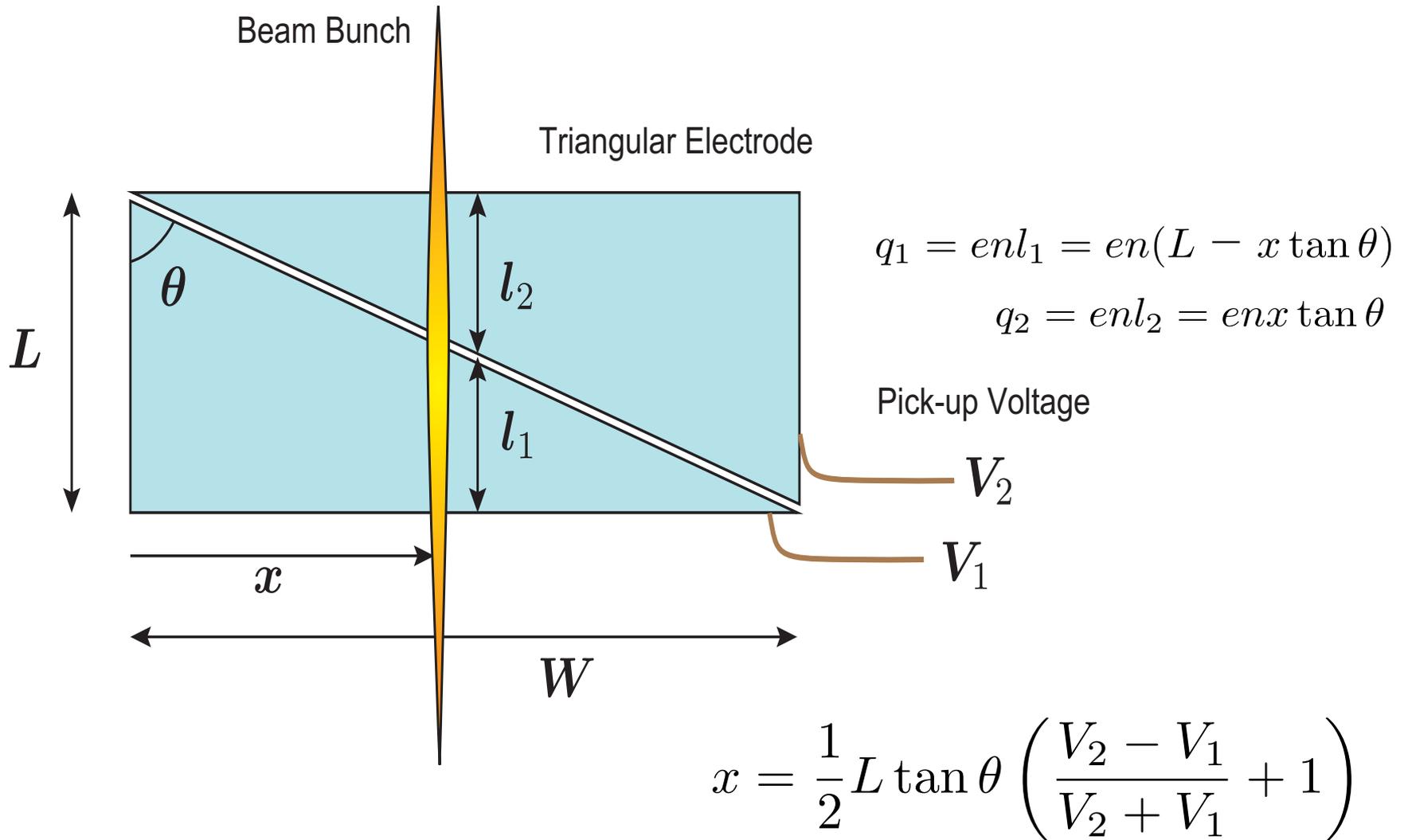
Beam position monitor

Electrostatic Position Monitor – The Principle

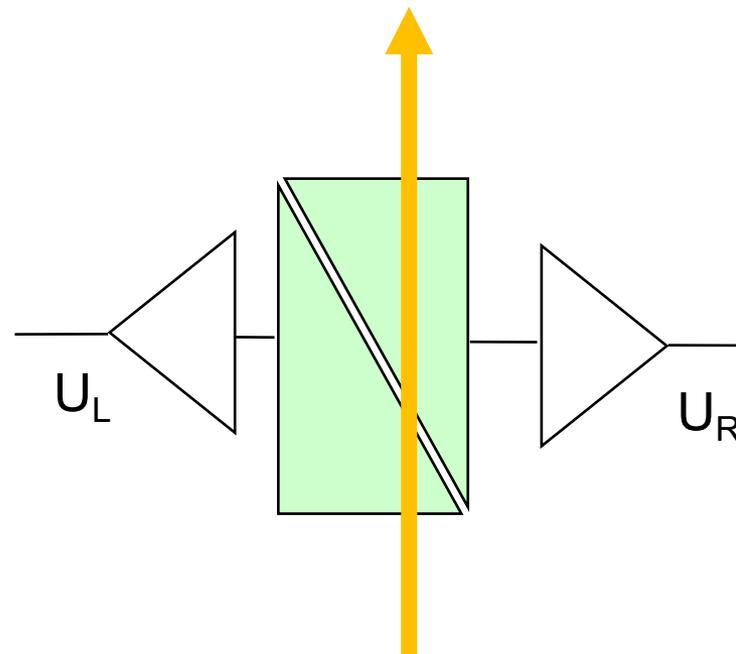
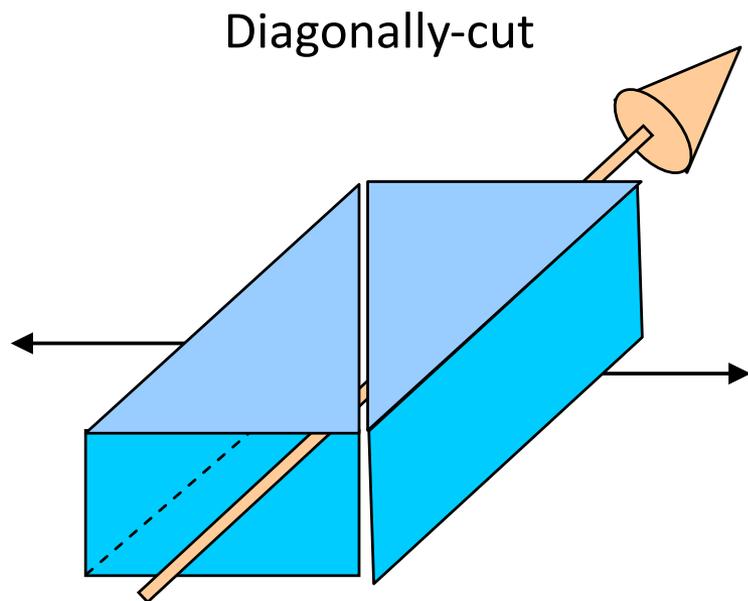
- Intercept “beam image current” in the vacuum chamber on two isolated (capacitive) pickups.
- shoebox pickups, stripline directional couplers....
- Use RF electronics to shape the signals
- Digitize the individual pickup signals
- Compute the position from the pickup-signal difference
- Linearize the pickup response



Pick-up position monitor with triangular electrodes



“Shoebox” pick-up monitor



$$X \propto \frac{U_L - U_R}{U_L + U_R} = \frac{\Delta U}{\Sigma U}$$

Advantage: Very linear, low frequency dependence
i.e. position sensitivity S is constant

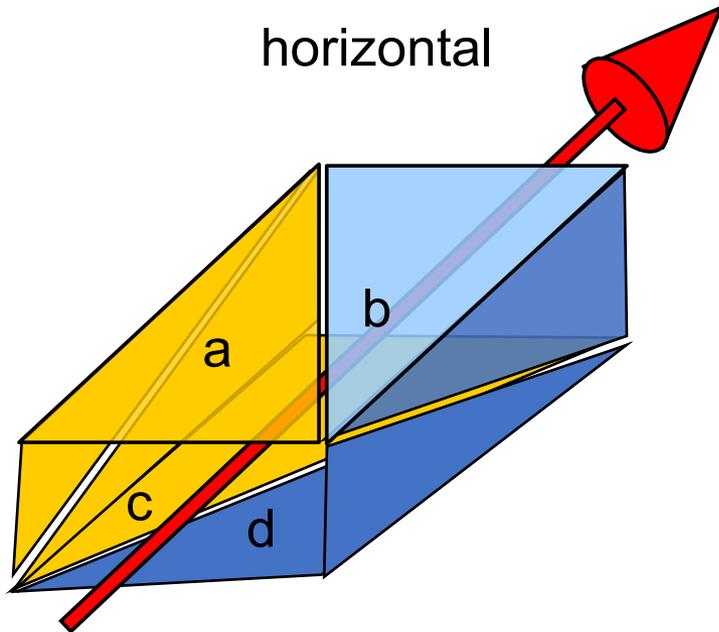
Disadvantage: Large size, complex mechanics

Usage: proton synchrotron
frf < 10MHz

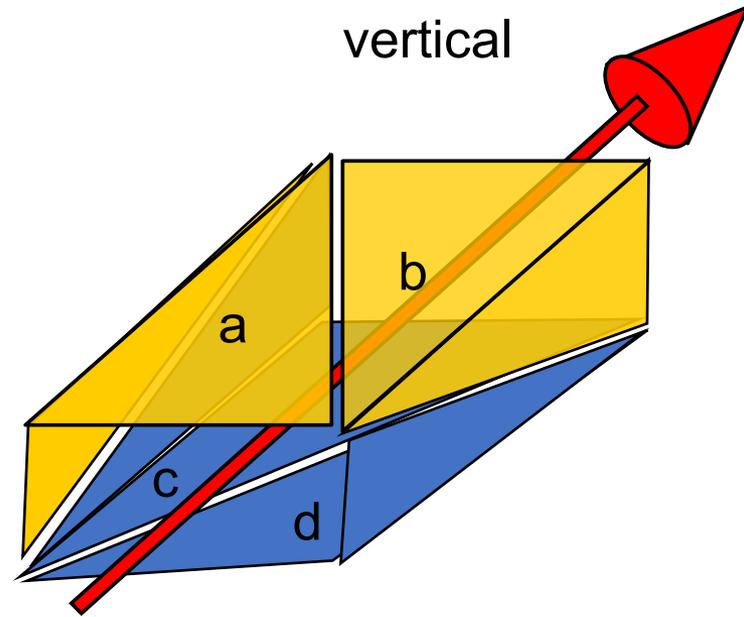
Calibration is required before installing.

Simultaneous horizontal and vertical measurement

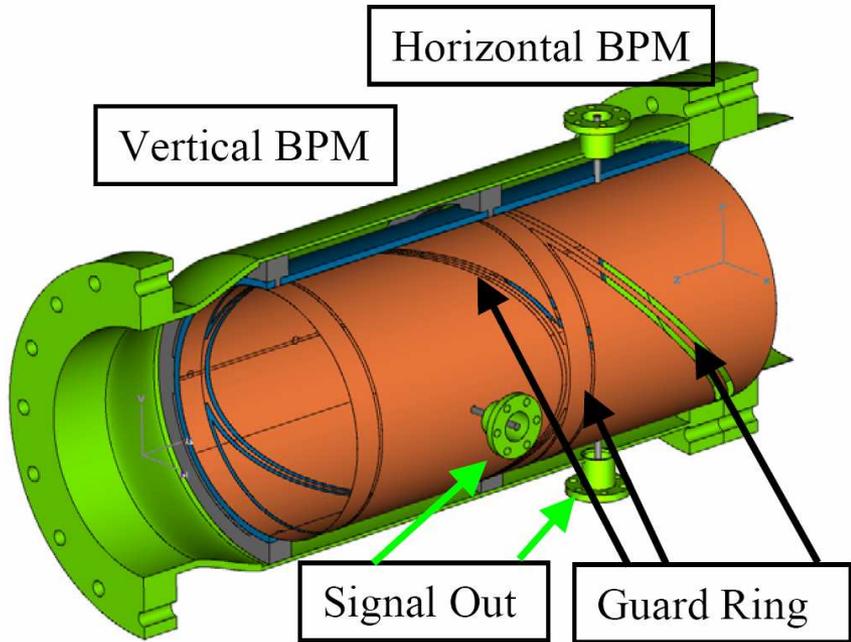
- Horizontal and vertical position at once
- 4 electrodes



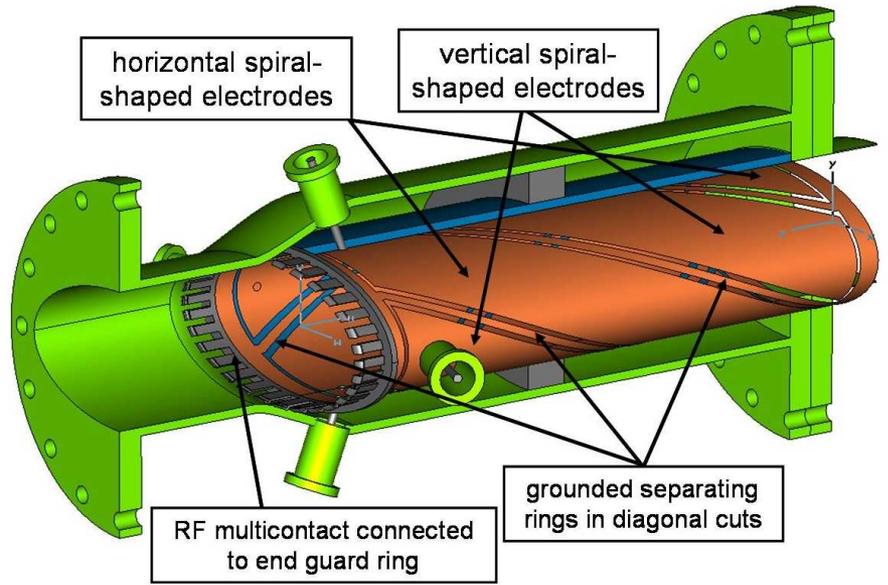
$$X = \frac{(U_a + U_c) - (U_b + U_d)}{\Sigma U}$$



$$Y = \frac{(U_a + U_b) - (U_c + U_d)}{\Sigma U}$$



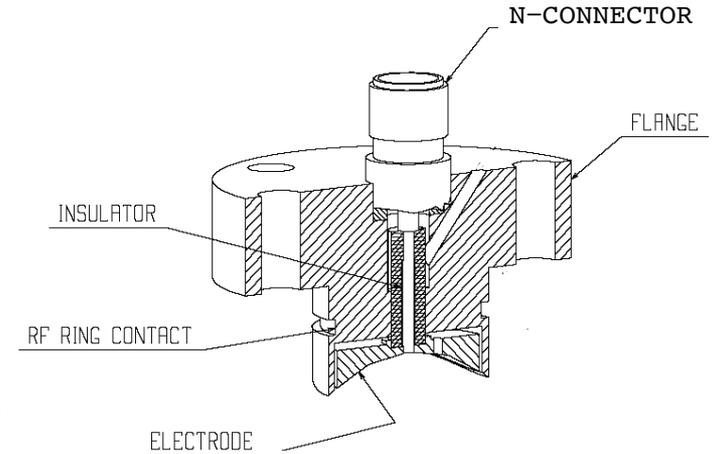
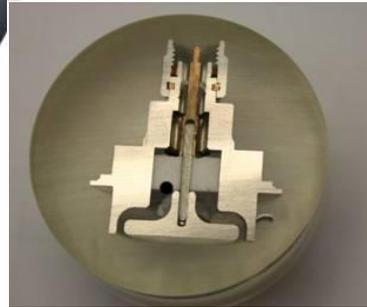
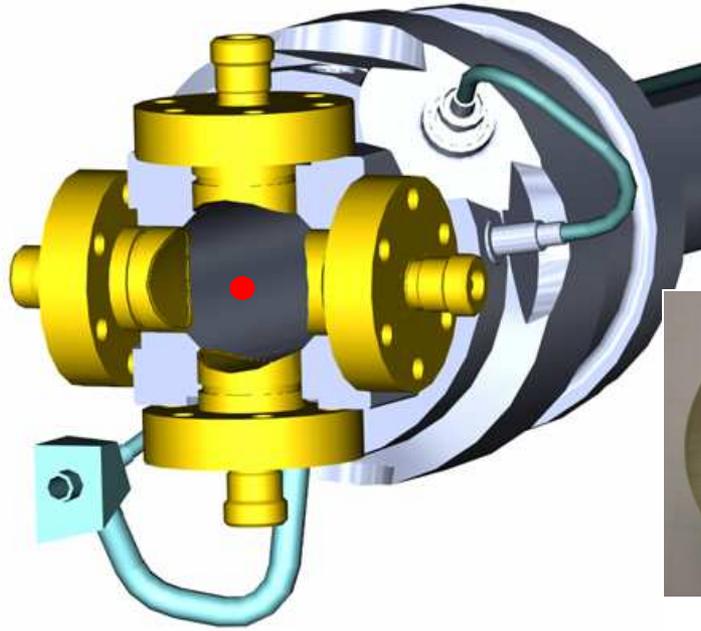
Linear-cut BPM in cylindrical geometry



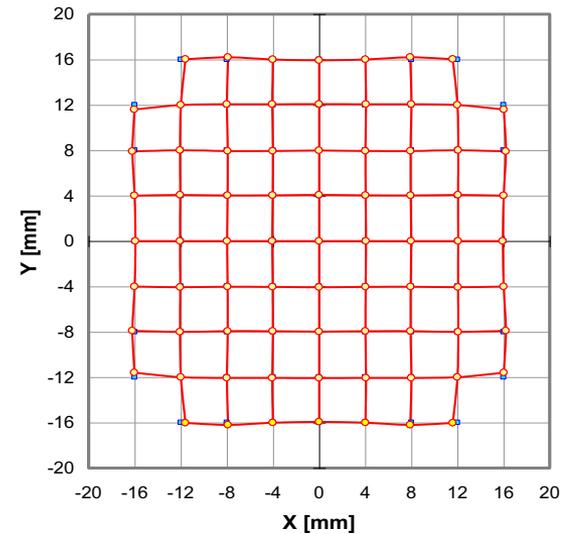
Wounded strip geometry

Button pick-up BPM

The installation of the curved $\text{\O} 24$ mm button BPMs at the LHC beam pipe of $\text{\O} 50$ mm.



BPM used at LHC

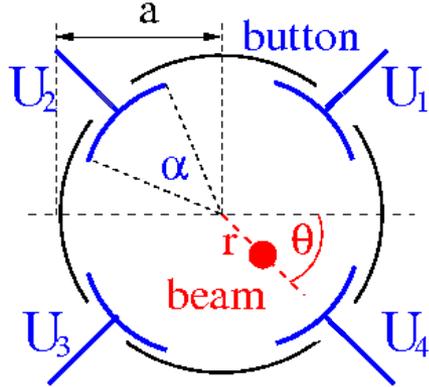


calibration map after correction

Button BPM – example for synchrotron light sources

The button BPM can be rotated by 45° to avoid exposure by synchrotron light:

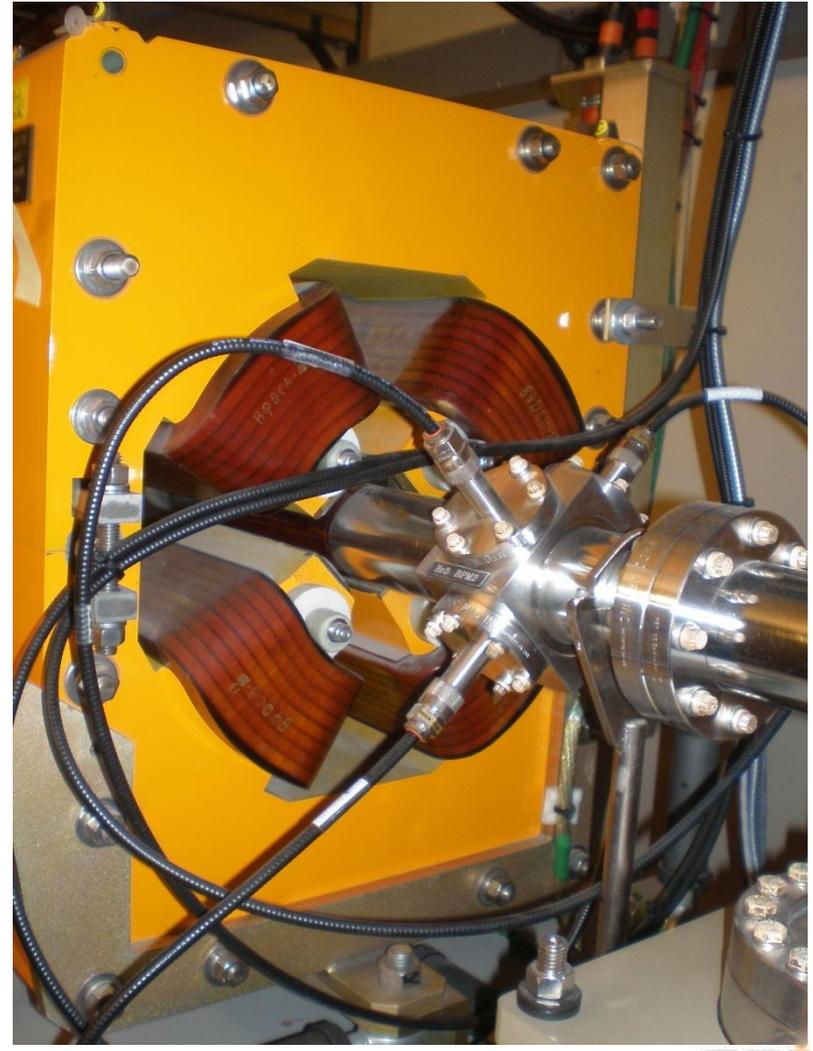
Frequently used at boosters for light sources



$$\text{horizontal: } x = \frac{1}{S} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

$$\text{vertical: } y = \frac{1}{S} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

Example: Booster of ALS, Berkeley

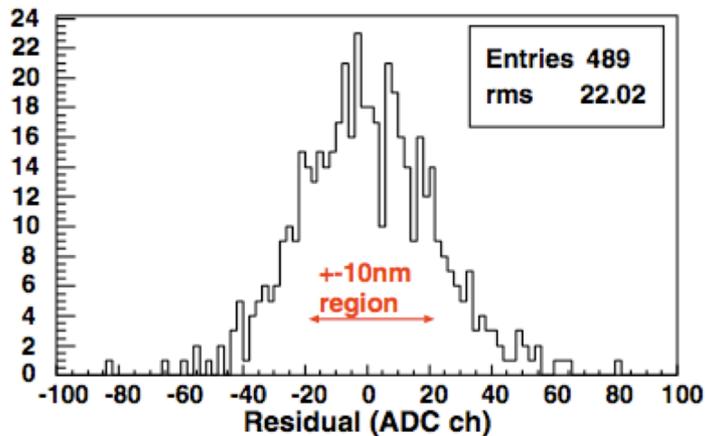
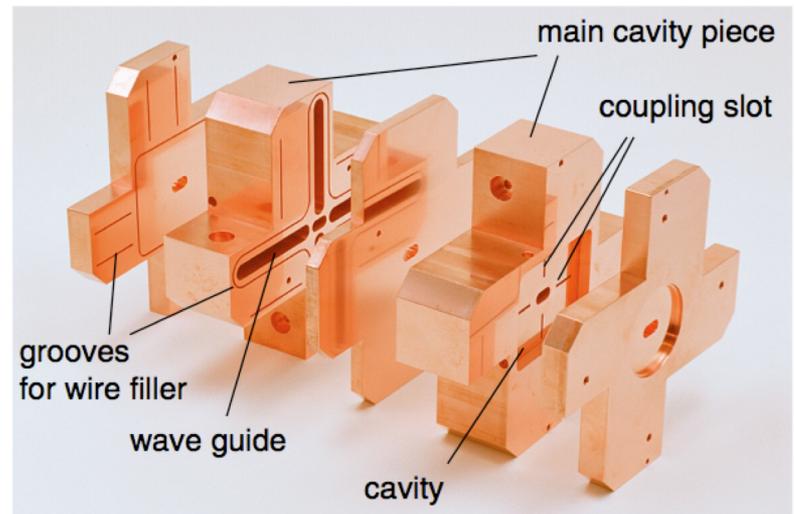
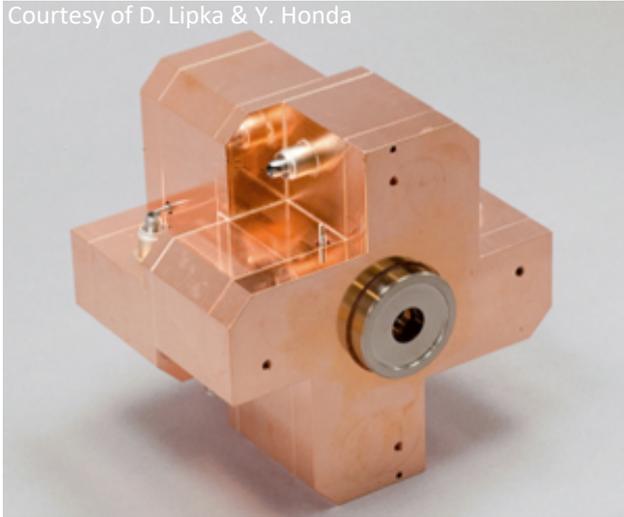


Today's State of the Art BPMs

Prototype BPM for ILC Final Focus

- Required resolution of 2nm (nano!) in a 6×12mm diameter beam pipe
- Achieved World Record (so far!) resolution of 8.7nm at ATF2 (KEK, Japan)

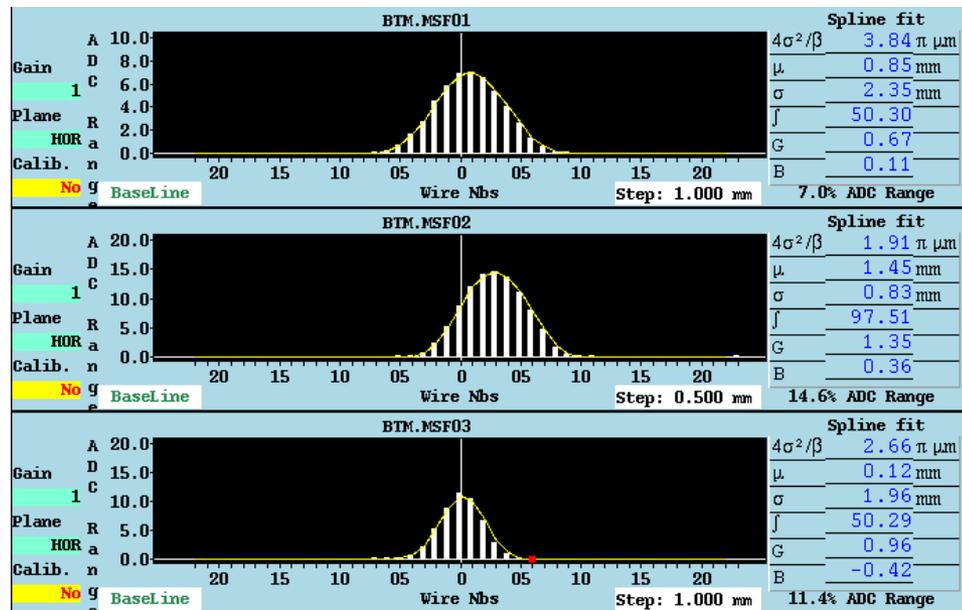
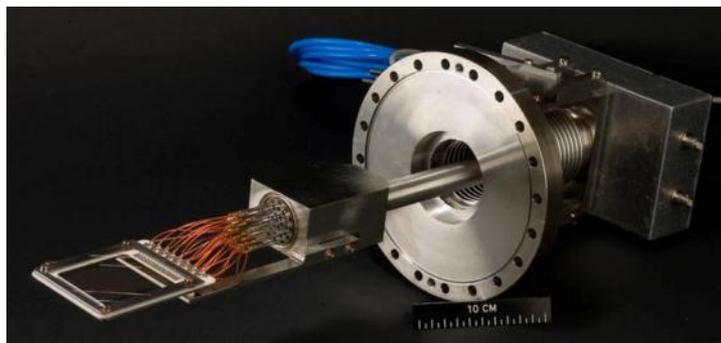
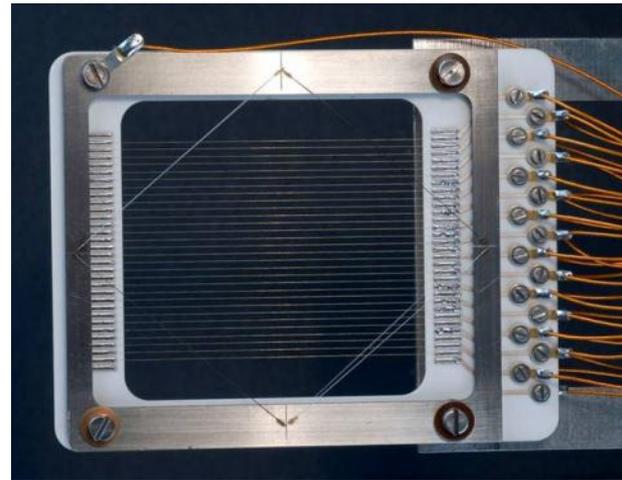
Courtesy of D. Lipka & Y. Honda



Beam profile monitor

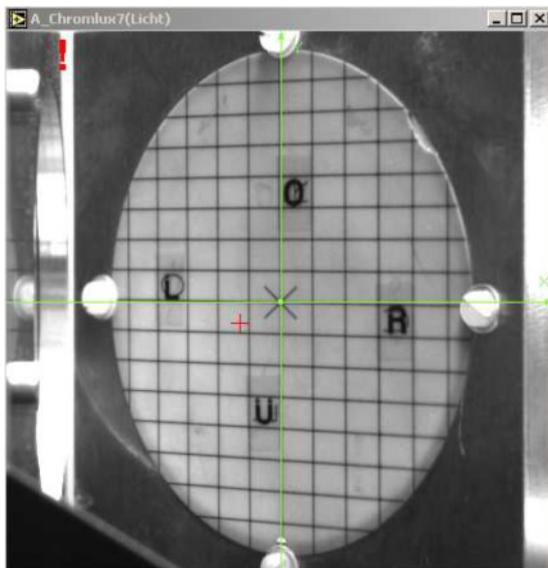
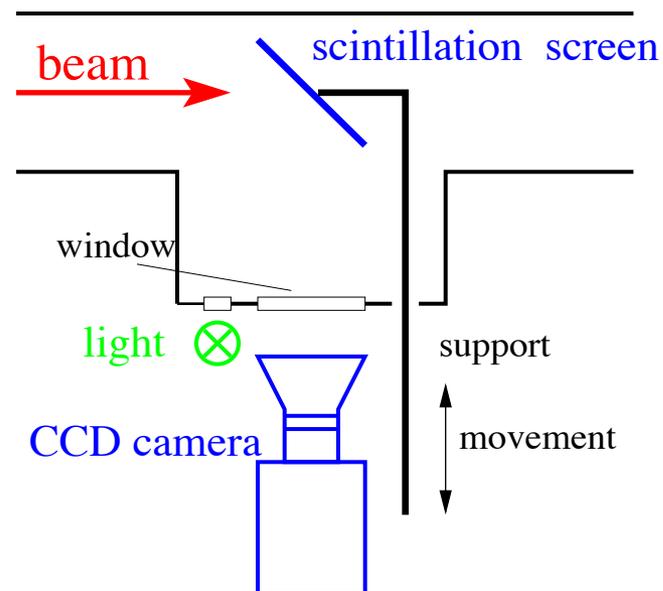
Secondary Electron eMission (SEM) Grids

- When the beam passes through, secondary electrons are emitted from a wire, proportional to beam intensity
- The current flowing back onto the wires is measured using one amplifier/ADC chain for each wire
- Very high sensitivity, semi-transparent
- Good absolute measurement
- Spatial resolution limited by wire spacing to $\lesssim 0.25\text{mm}$
- Dynamic range: $\approx 10^6$



Scintillation screens

- Typically for setting-up with low intensities, screen thickness (mm)
- Sensitivities of different materials vary by orders of magnitudes

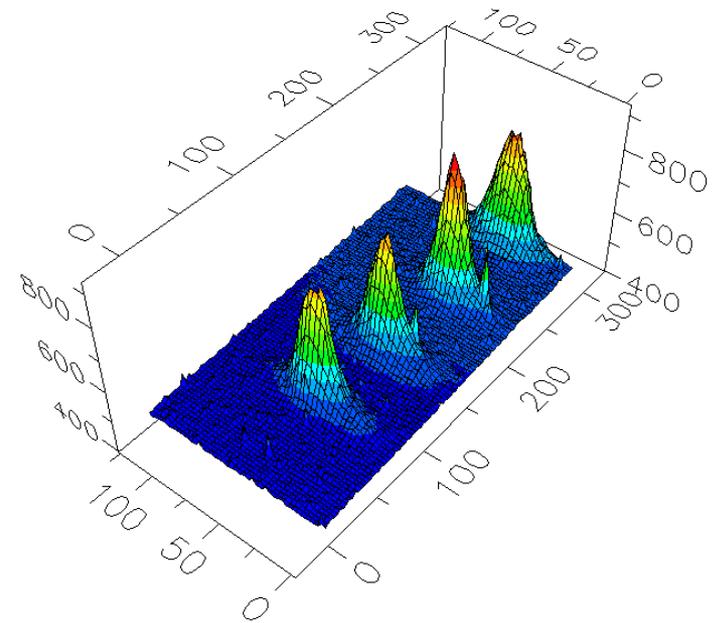
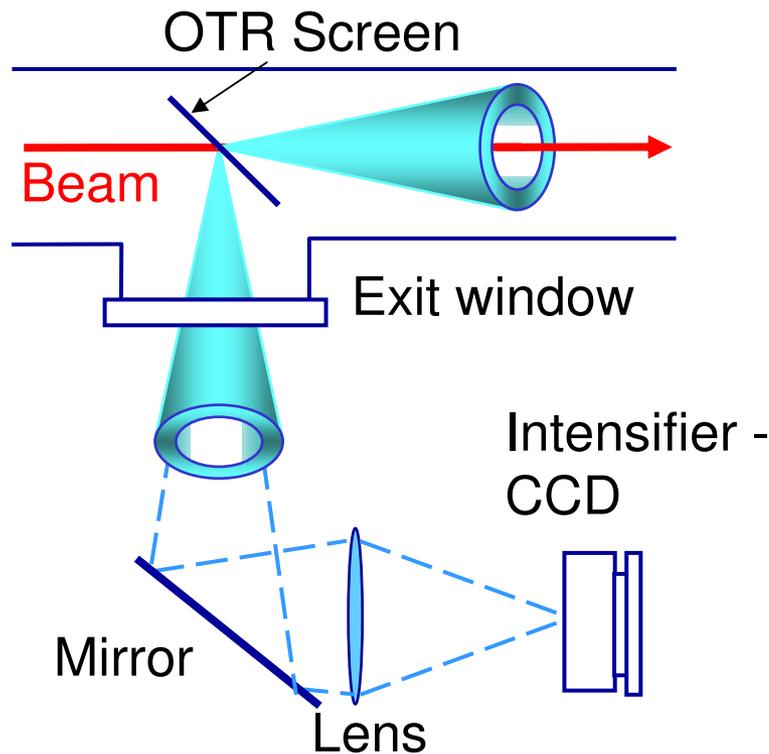


Properties of inorganic scintillators

Abbreviation	Material	Activator	max. emission	decay time
Quartz	SiO ₂	none	470 nm	< 10 ns
	CsI	Tl	550 nm	1 μs
Chromolux	Al ₂ O ₃	Cr	700 nm	100 ms
YAG	Y ₃ Al ₅ O ₁₂	Ce	550 nm	0.2 μs
	Li glass	Ce	400 nm	0.1 μs
P11	ZnS	Ag	450 nm	3 ms
P43	Gd ₂ O ₂ S	Tb	545 nm	1 ms
P46	Y ₃ Al ₅ O ₁₂	Ce	530 nm	0.3 μs
P47	Y ₂ Si ₅ O ₅	Ce&Tb	400 nm	100 ns

Optical Transmission Radiation (OTR) screens

- Radiation emitted when a charged particle beam goes through the interface of two media with different dielectric constants
- Surface phenomenon allows the use of very thin screens ($\sim 10\mu\text{m}$)
- much less intercepting, but requires higher intensity

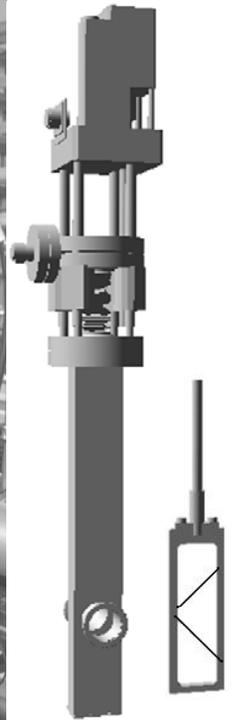
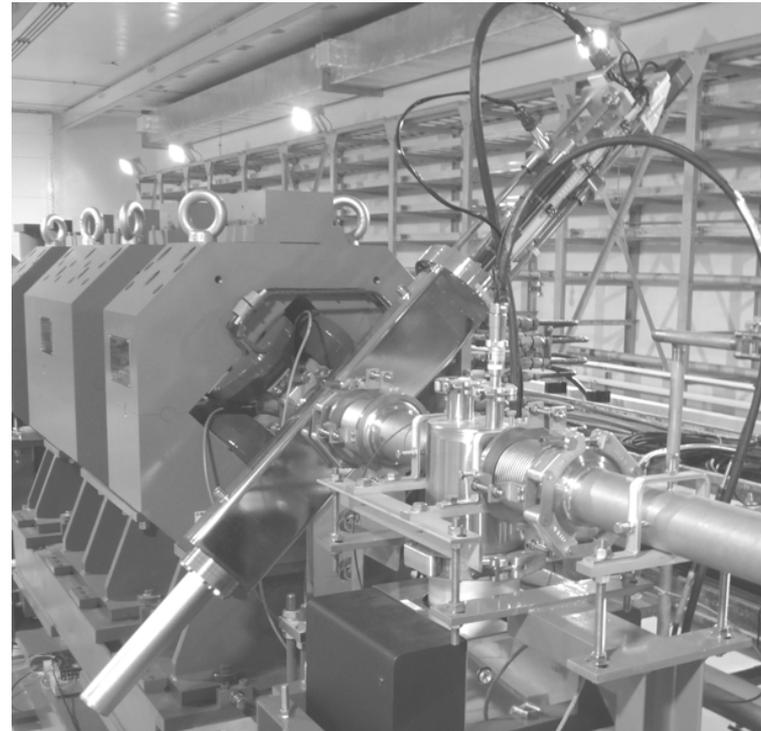
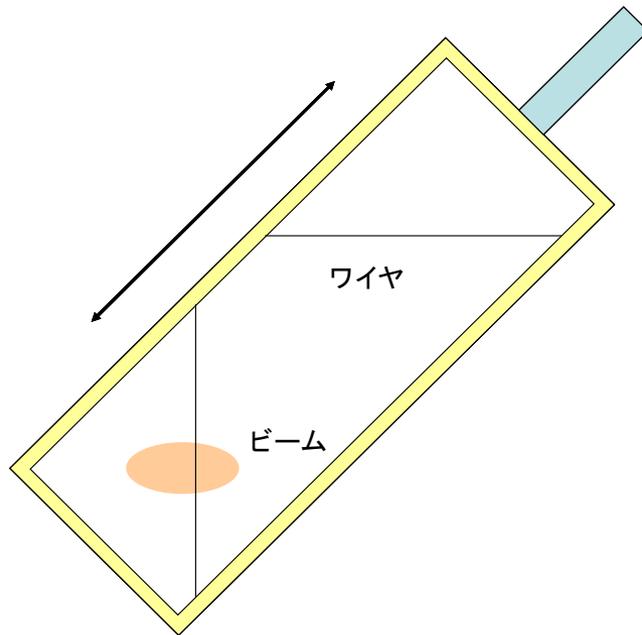


CERN SPS at injection

for electron accelerators

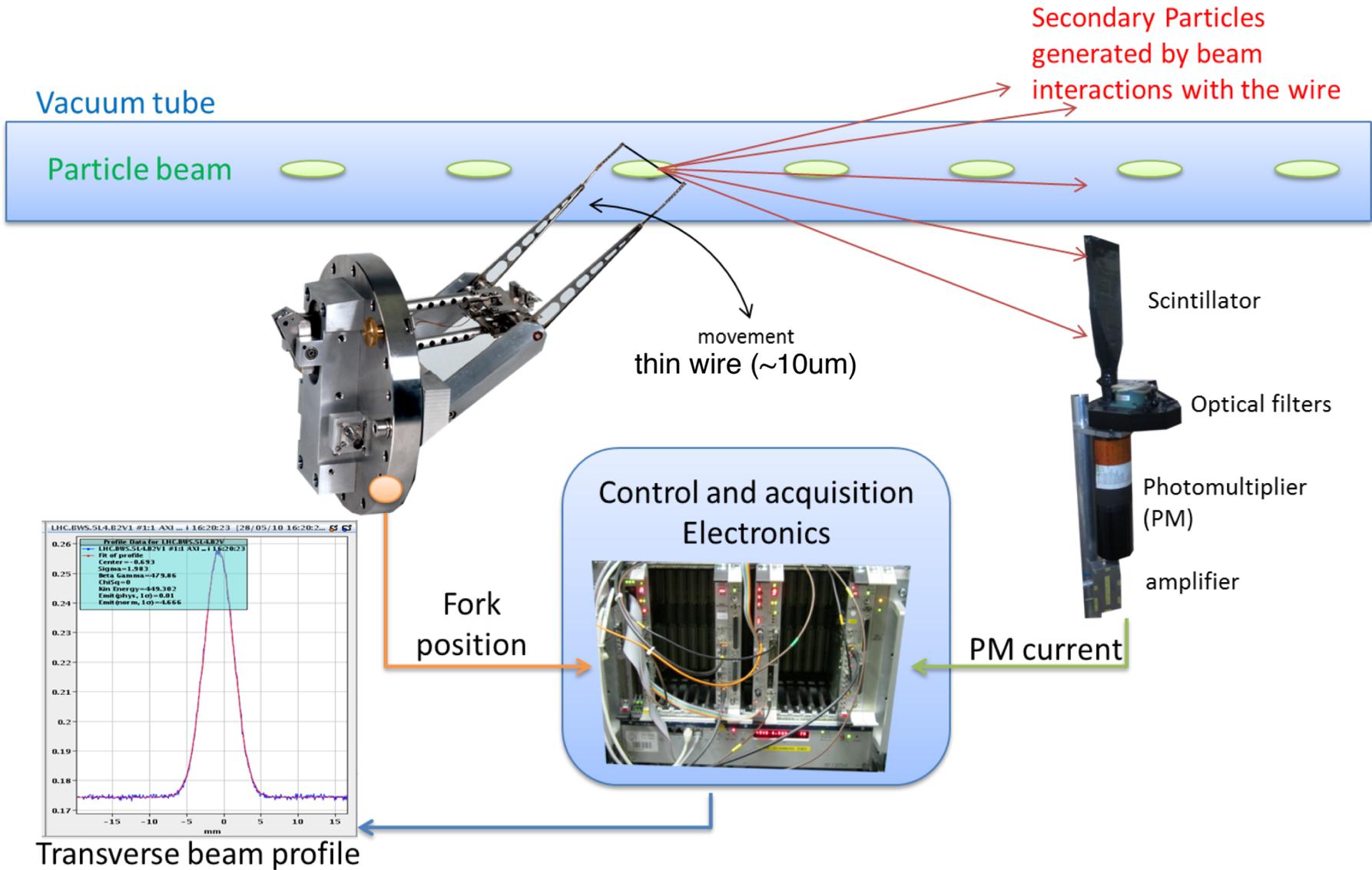
Wire scanners

WSM (J-Parc LINAC)



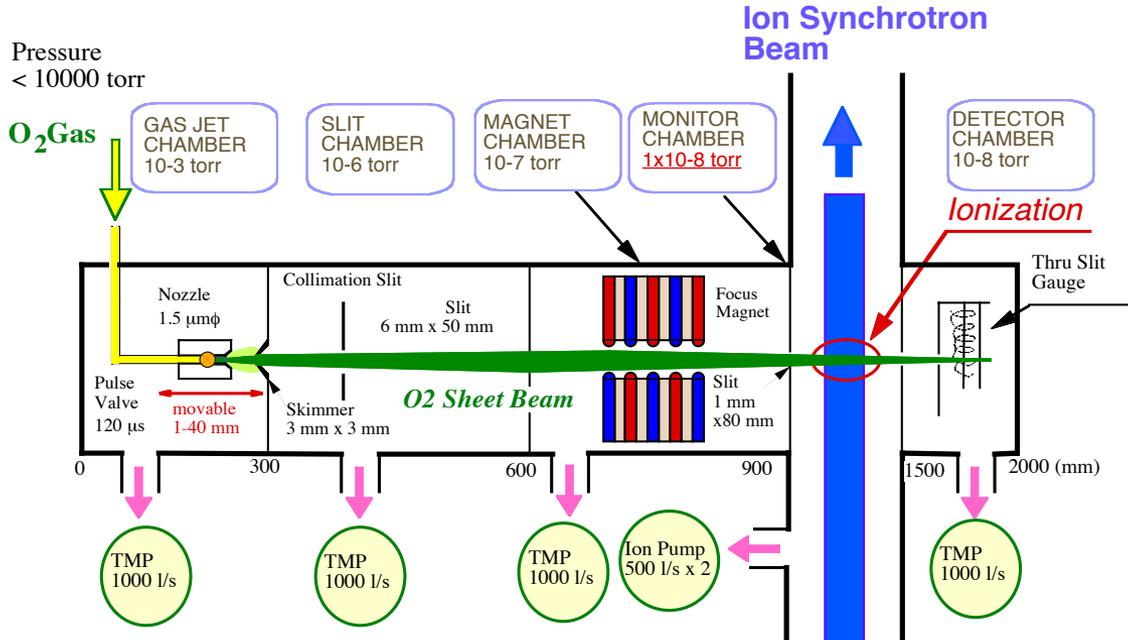
The wires are connected on a frame with 45deg, if the frame is installed with 45deg against the horizontal axis, both horizontal and vertical profiles can be measured in a stroke.

Wire scanners

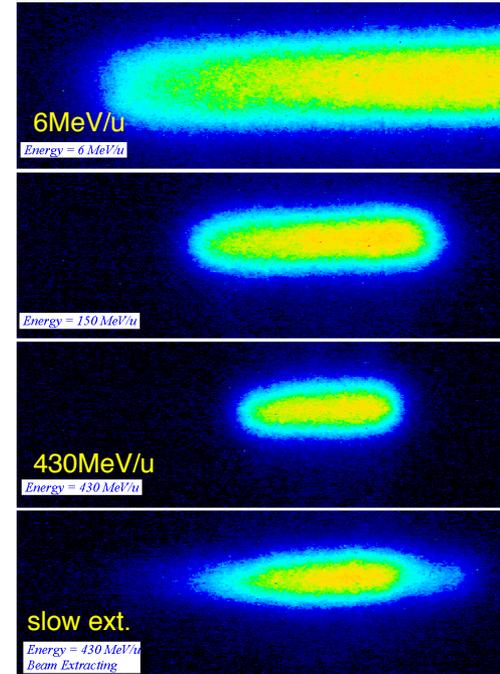
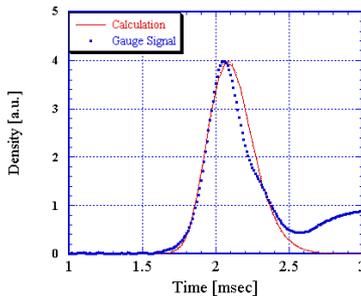
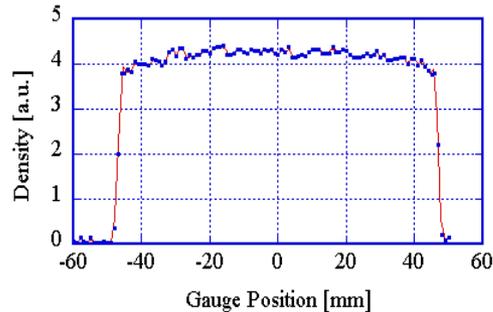


Gas sheet BPM

- non-destructive

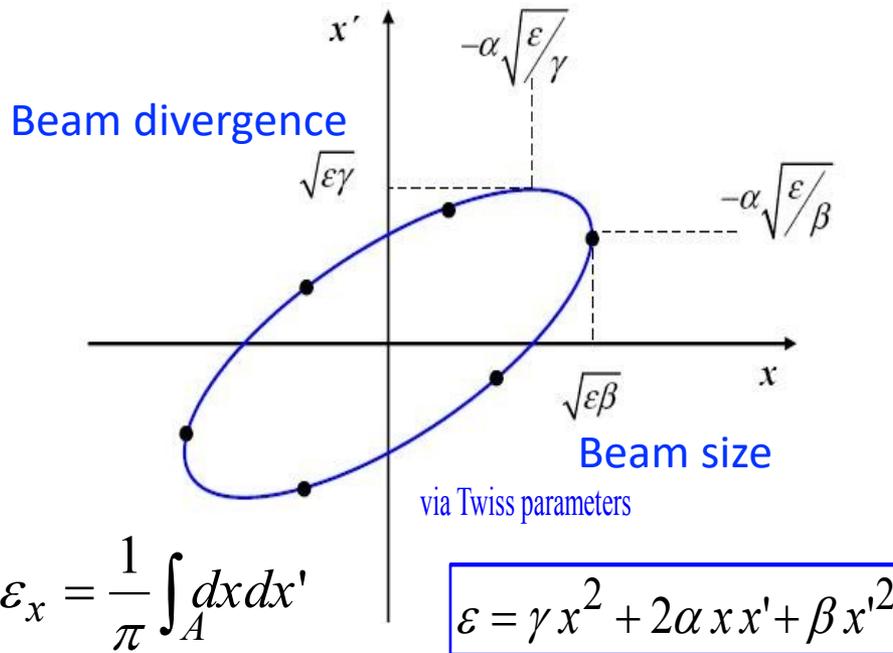


Thickness of O₂ sheet beam : ~1 mm



Profile images of HIMAC C⁶⁺ beam

Transverse emittance measurement



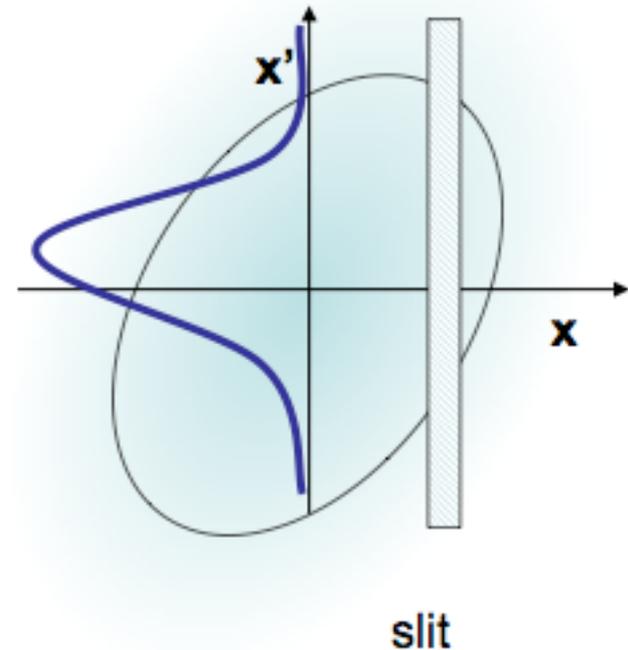
beam matrix

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} = \varepsilon \cdot \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix} \text{ with } \vec{x} = \begin{pmatrix} x \\ x' \end{pmatrix}$$

$$x_\sigma = \sqrt{\sigma_{11}} = \sqrt{\varepsilon\beta} \quad \text{and}$$

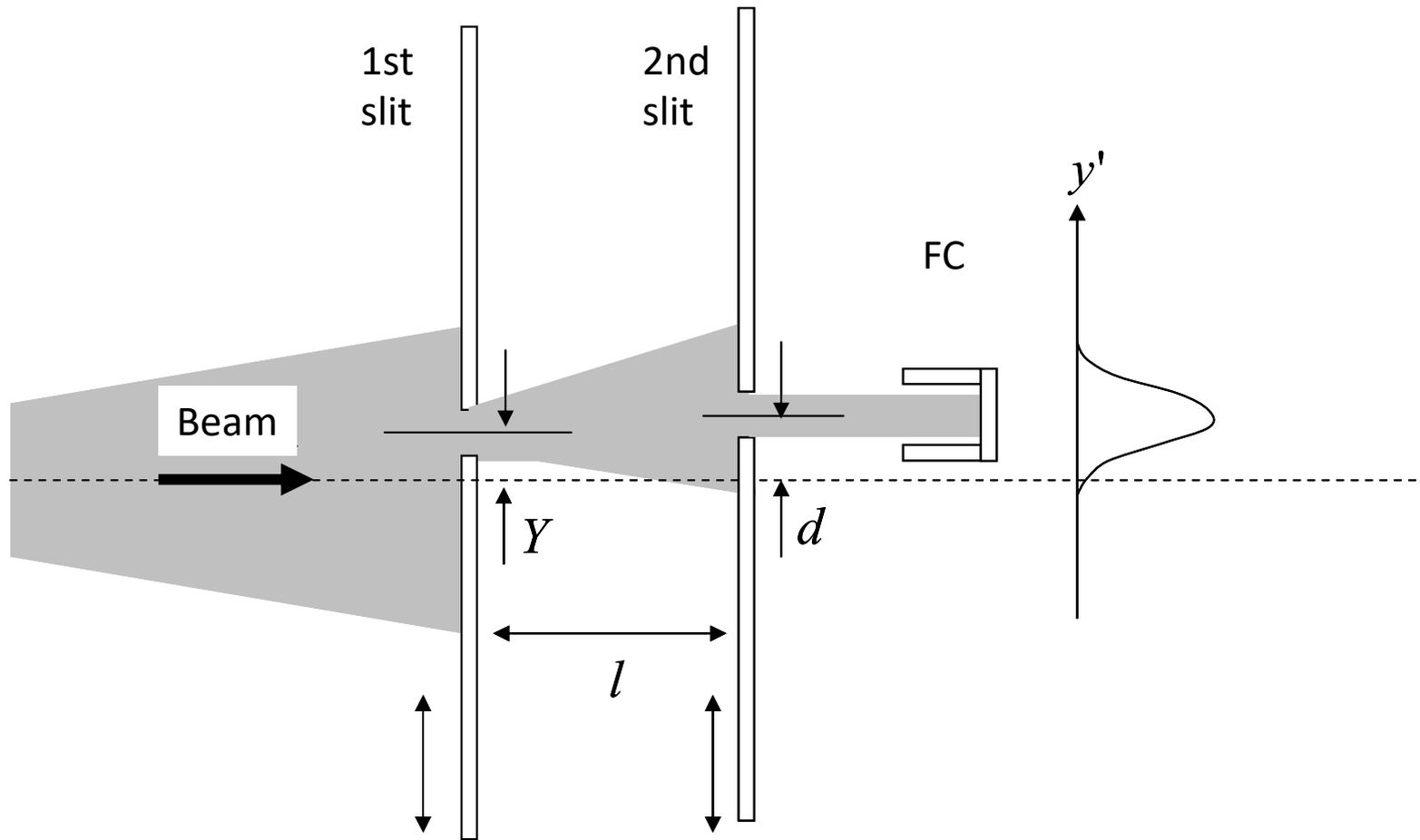
$$x'_\sigma = \sqrt{\sigma_{22}} = \sqrt{\varepsilon\gamma}$$

- If for each beam particle we plot its position and its transverse angle we get a particle distribution whose boundary is an ellipse.
- The projection onto the x axis is the beam size.



- If we place a slit into the beam we cut out a small vertical slice of phase space.
- Converting the angles into position through a drift space allows to reconstruct the angular distribution at the position defined by the slit.

Double-Slit emittance measurement

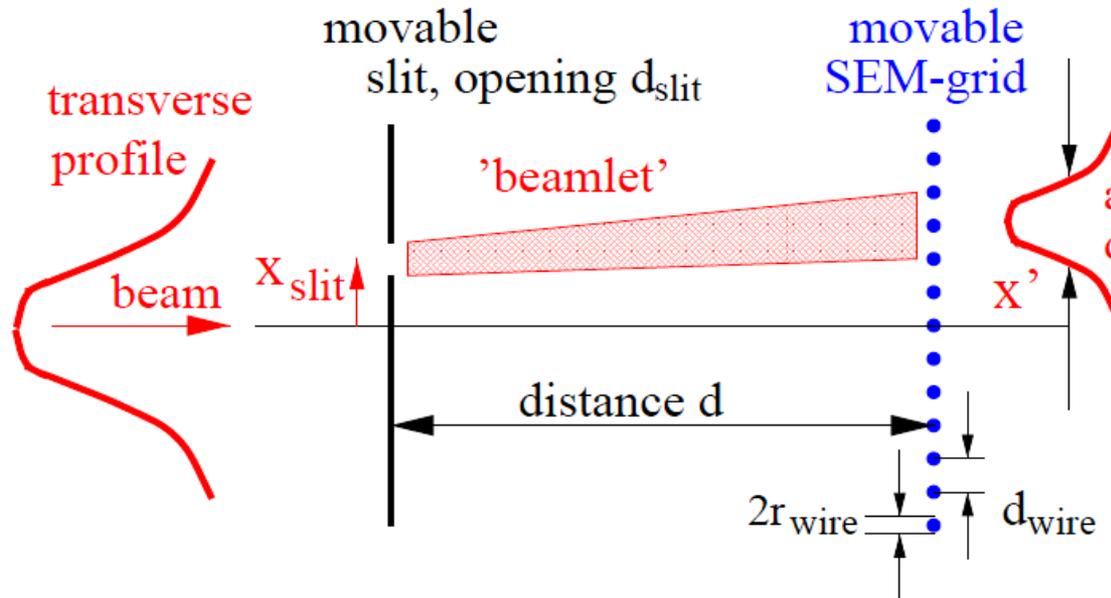


Slit-Grid emittance measurement

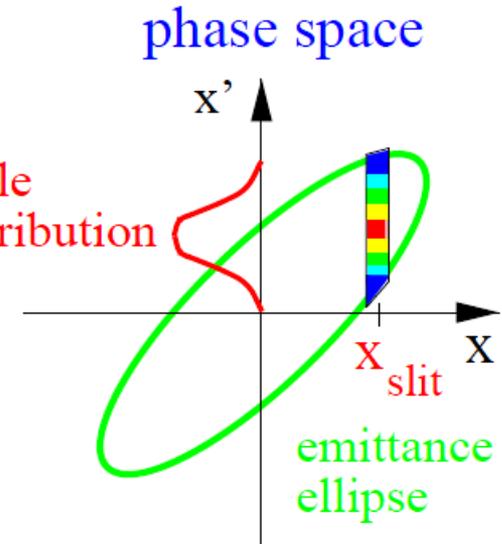
Slit-Grid: Direct determination of position and angle distribution.

Used for protons/heavy ions with $E_{kin} < 100 \text{ MeV/u} \Leftrightarrow \text{range } R < 1 \text{ cm}$.

Hardware



Analysis



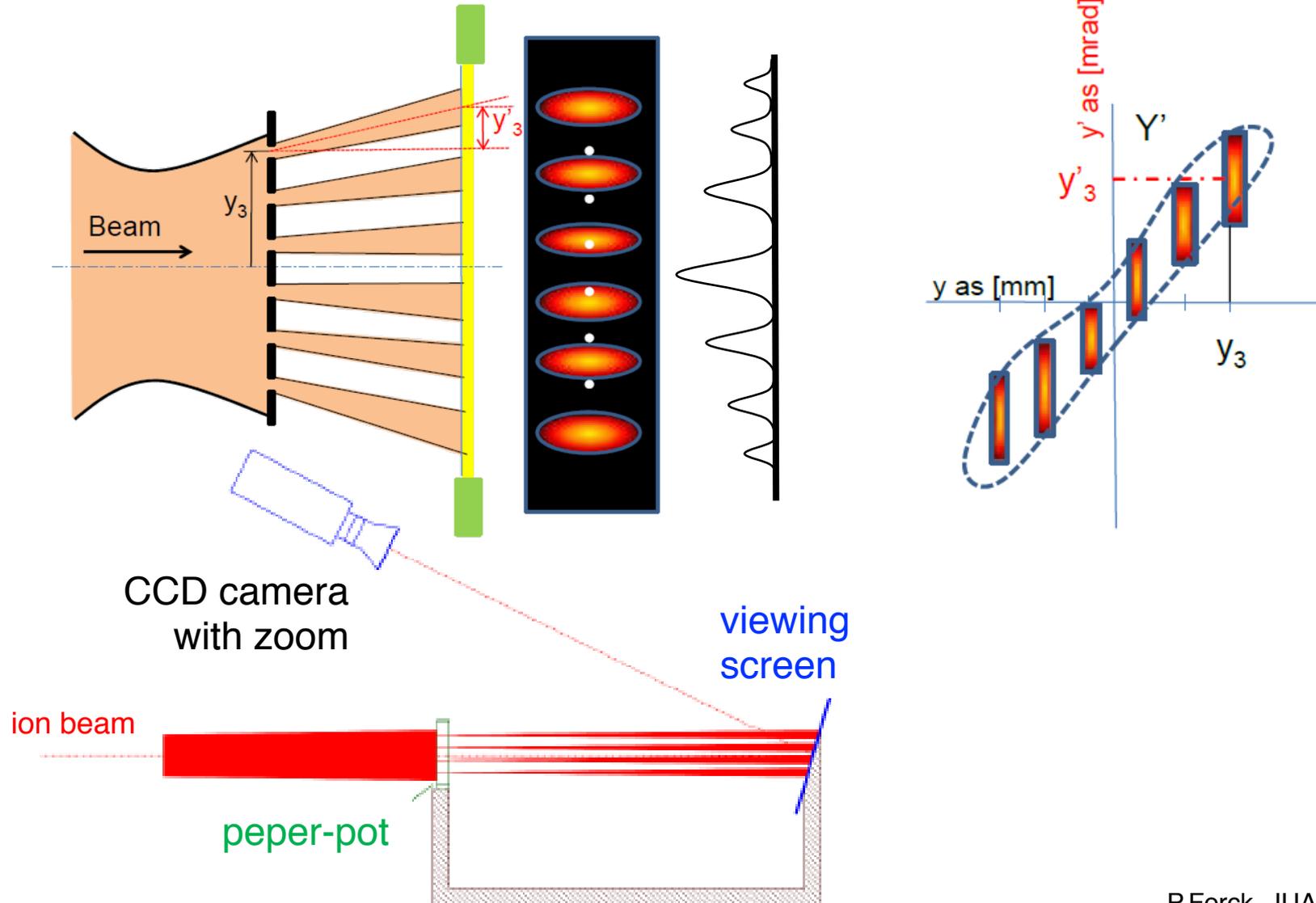
Slit: position $P(x)$ with typical width: 0.1 to 0.5 mm

Distance: 10 cm to 1 m (depending on beam velocity)

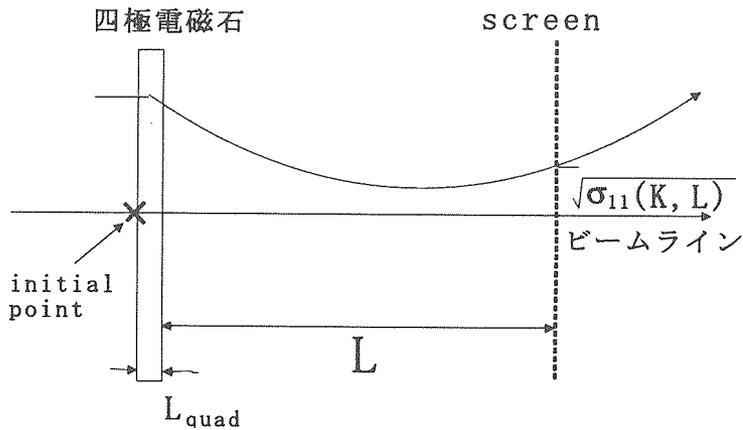
SEM-Grid: angle distribution $P(x')$

Pepper-pot emittance measurement

Advantage: Single-shot measurement



Emittance measurement : Quadrupole scan technique (Q-scan)



Transfer matrix of the drift space

$$\mathbf{R}_{\text{drift}} = \begin{pmatrix} 1 & L \\ 0 & 1 \end{pmatrix}$$

Transfer matrix of the quadrupole

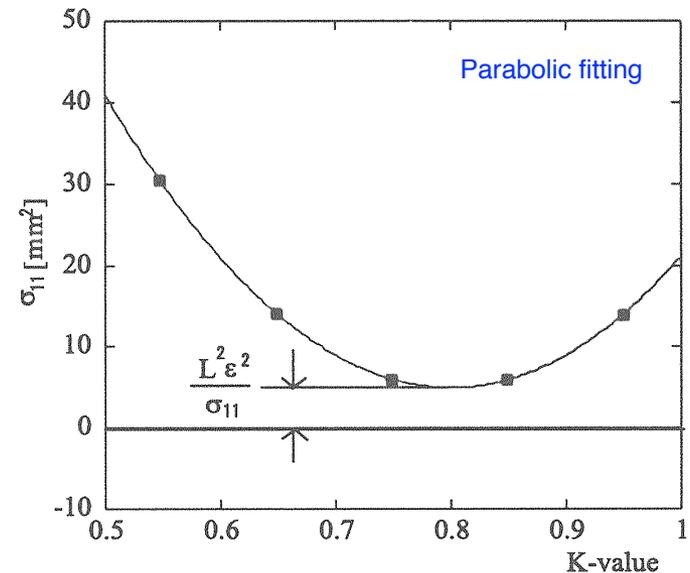
$$\mathbf{R}_{\text{quad}} = \begin{pmatrix} 1 & 0 \\ -K & 1 \end{pmatrix} \quad K = \frac{\partial B_y}{\partial x} \frac{L_{\text{quad}}}{(B\rho)}$$

$$\mathbf{R}(K, L) = \mathbf{R}_{\text{drift}} \mathbf{R}_{\text{quad}} = \begin{pmatrix} 1 - KL & L \\ -K & 1 \end{pmatrix}$$

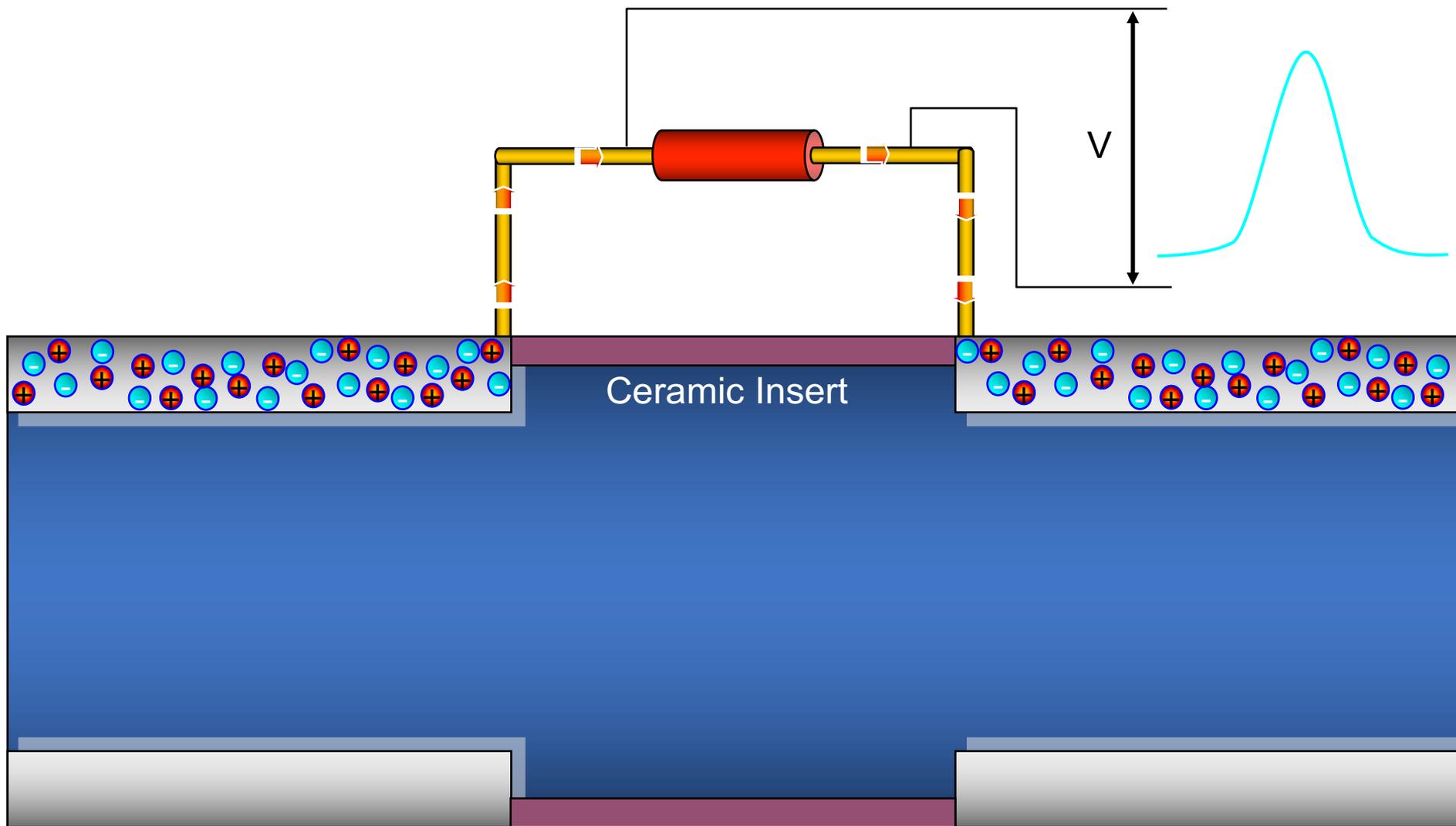
$$\begin{aligned} \sigma(K, L) &= \mathbf{R}(K, L) \sigma_0 \mathbf{R}^t(K, L) \\ &= \begin{pmatrix} 1 - KL & L \\ -K & 1 \end{pmatrix} \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} \\ &\quad \times \begin{pmatrix} 1 - KL & -K \\ L & 1 \end{pmatrix} \end{aligned}$$

$$\begin{aligned} \sigma_{11}(K, L) &= (1 - KL)^2 \sigma_{11} \\ &\quad + 2L(1 - KL) \sigma_{12} + L^2 \sigma_{22} \end{aligned}$$

Measured beam size as a function of the quadrupole field strength

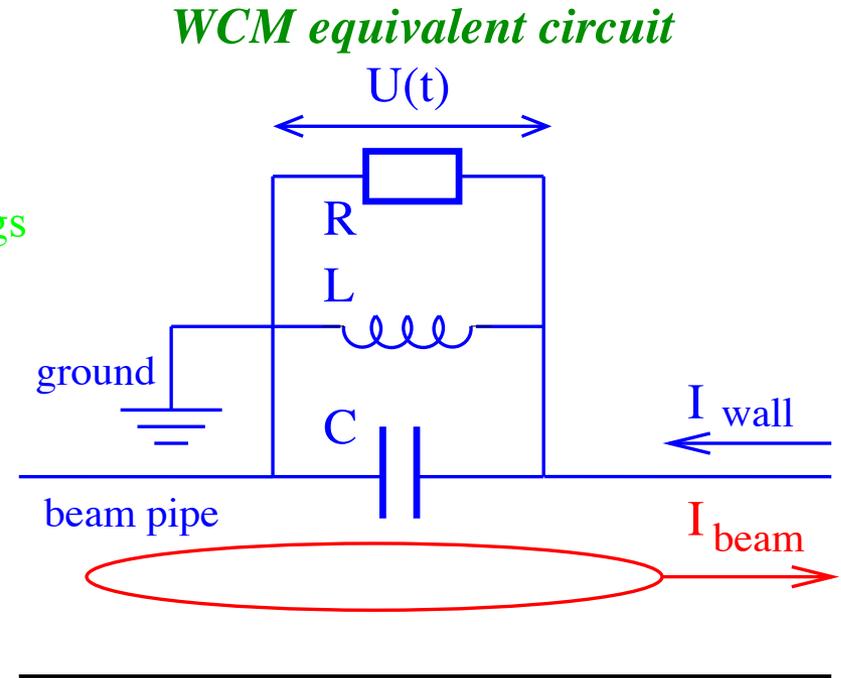
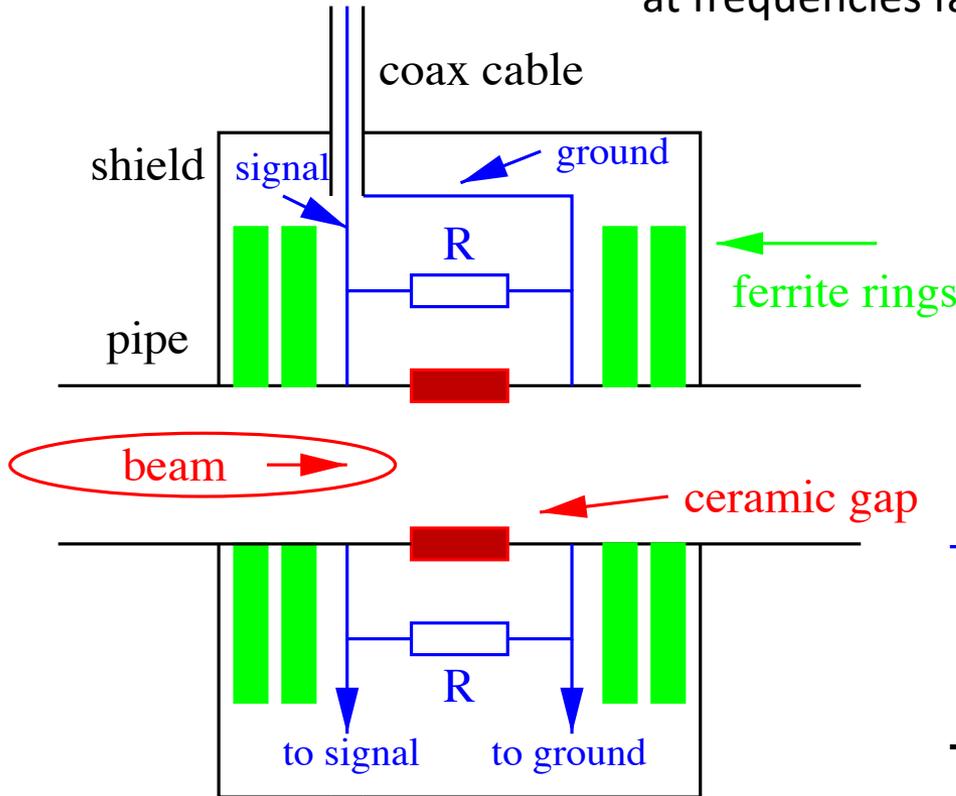


Wall Current Monitor – The Principle



Wall current monitors

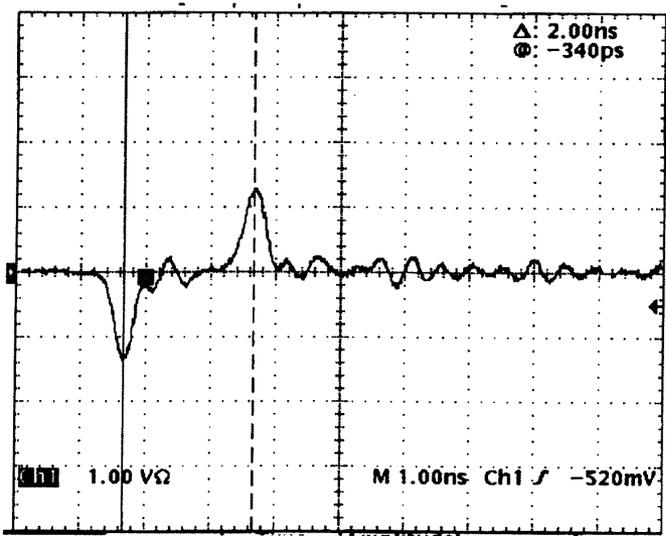
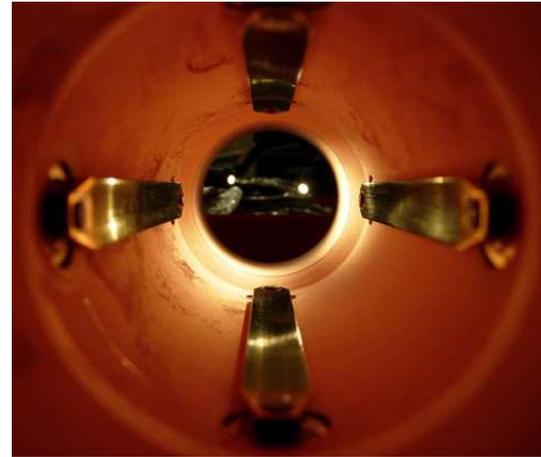
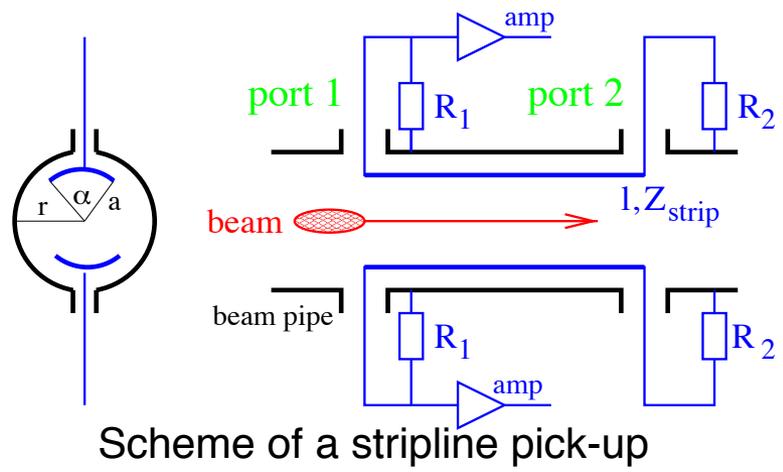
WCM can observe the short bunch shape of electrons at frequencies far beyond the few 100 MHz.



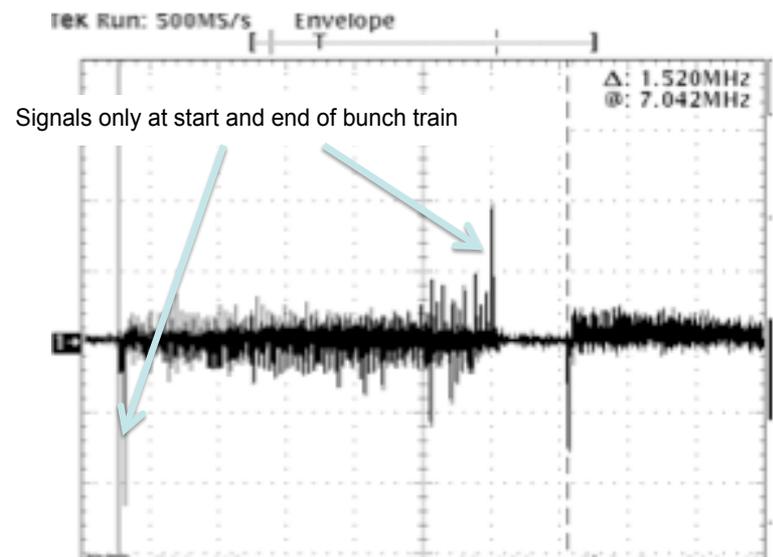
When the beam is not at the centre of the vacuum chamber, the wall-current will be unequally distributed around the circumference of the chamber.

The signals are picked-up separately → Beam position monitoring

Stripline pick-ups ~ bunch monitor



Single shot signal from a 30 cm stripline pick-up ($t=2L/c$)



Multibunch signal $L=30\text{cm}$, bunch spacing 60cm (2ns)

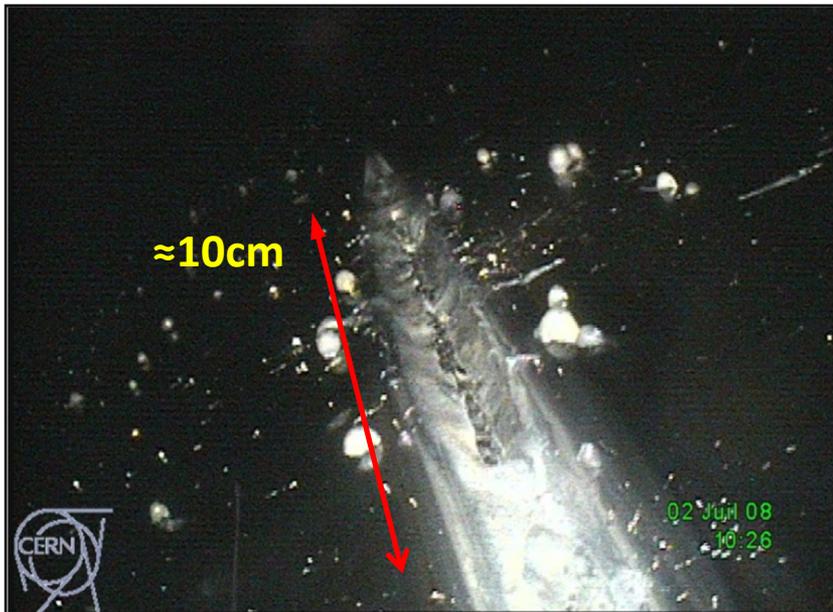
Beam loss monitors

Beam Loss

secondary products from electromagnetic or hadronic shower

Role of beam loss monitor :

- Protect the machine from damage and activation
- Dump the beam to avoid magnet quenches (for superconducting magnets)
- Diagnostic tool to improve the performance of the accelerator



SPS incident

- June 2008

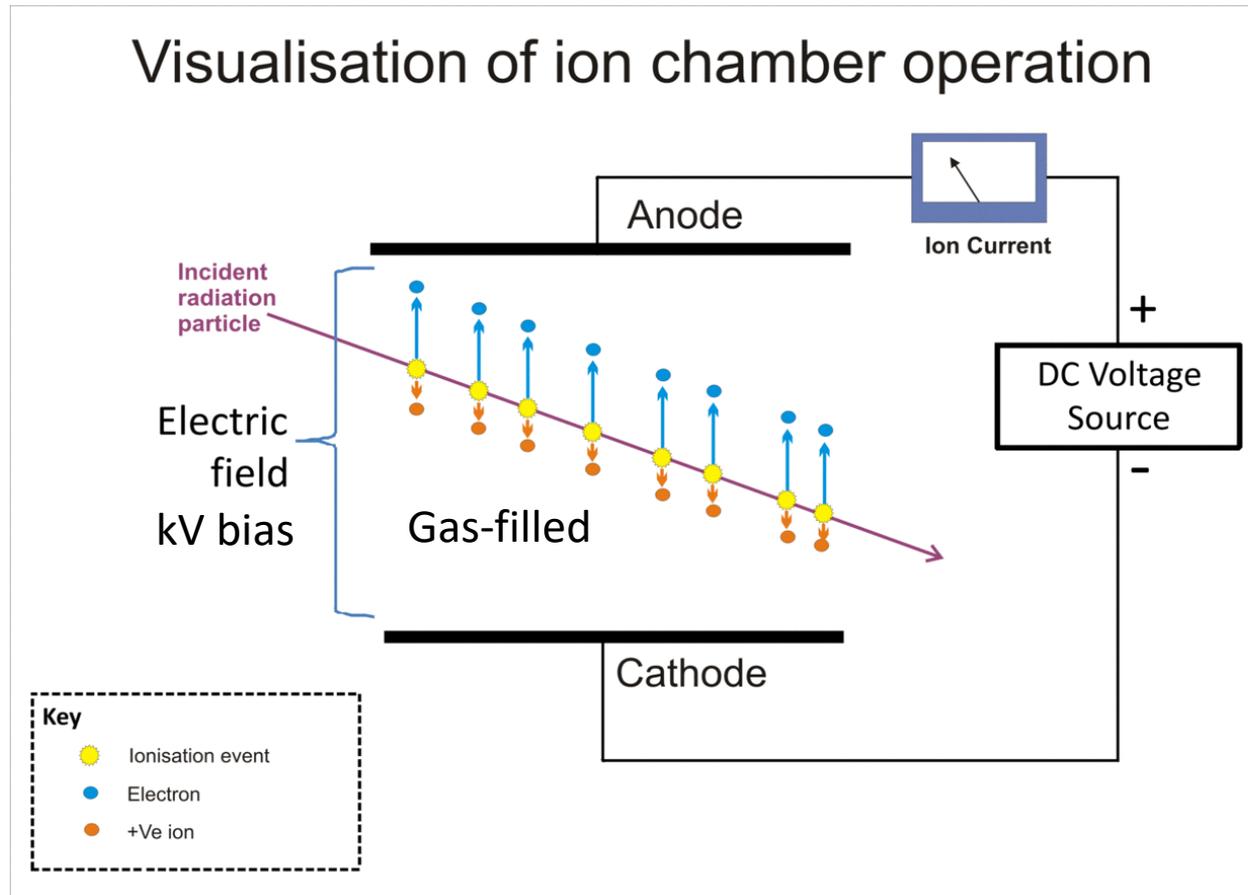
- 2MJ beam lost at 400MeV



Beam Loss Monitors (BLM) - Ionization chambers

Ionization chambers (charge detection)

- Dynamic range of $< 10^8$
- Slow response (μs) due to ion drift time

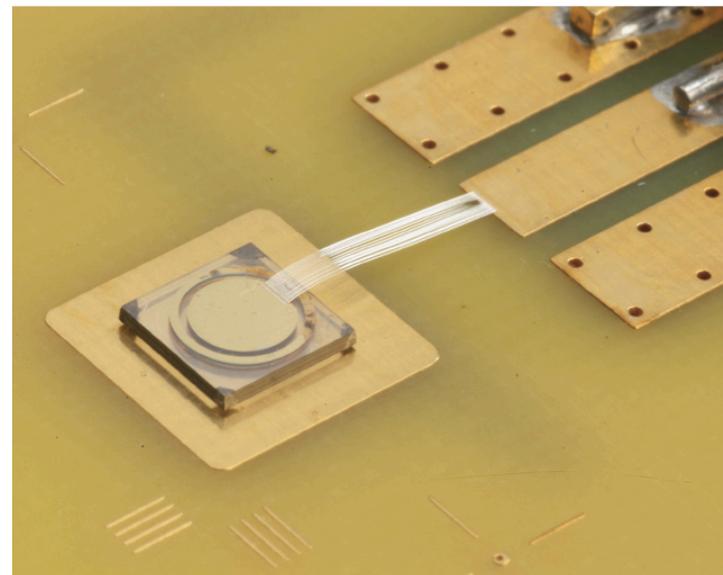
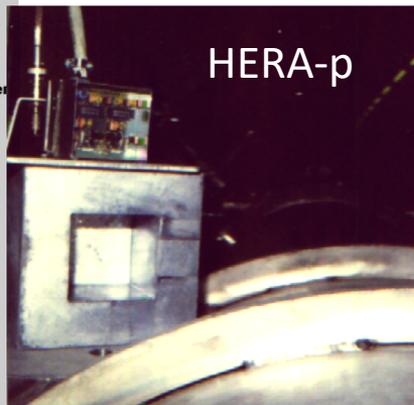
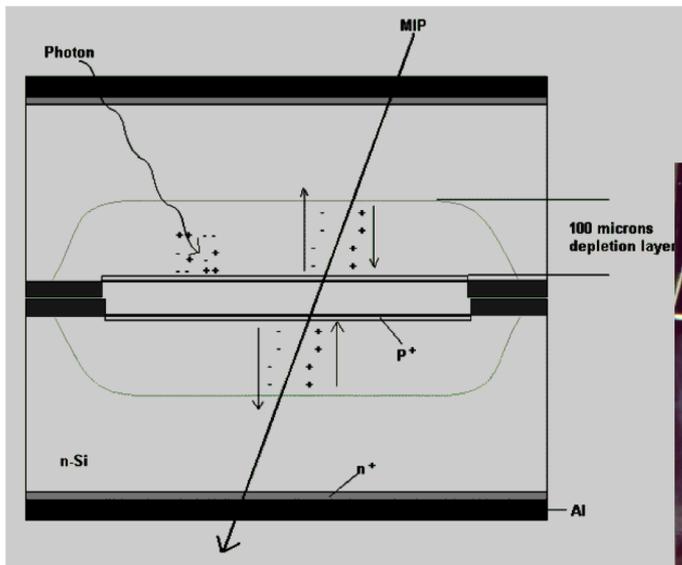


LHC BLM system



- Main purpose: prevent damage and quench
- 3600 Ionization chambers
- reaction time : $\sim 100\mu\text{s}$
- radiation hard : $\sim \text{kGy}$

Beam Loss Monitors



PIN photodiode (solid state ionisation chamber)

Count detection

Detect coincidence of ionising particle crossing photodiodes

Insensitive to photons from synchrotron radiation

Count rate proportional to beam loss with speed limited by integration time

Can distinguish between photon & ionising particles

Dynamic range of up to 10^9

Diamond Detectors

- Fast & sensitive
- Used in LHC to distinguish bunch by bunch losses
- Work **in** cryogenic conditions

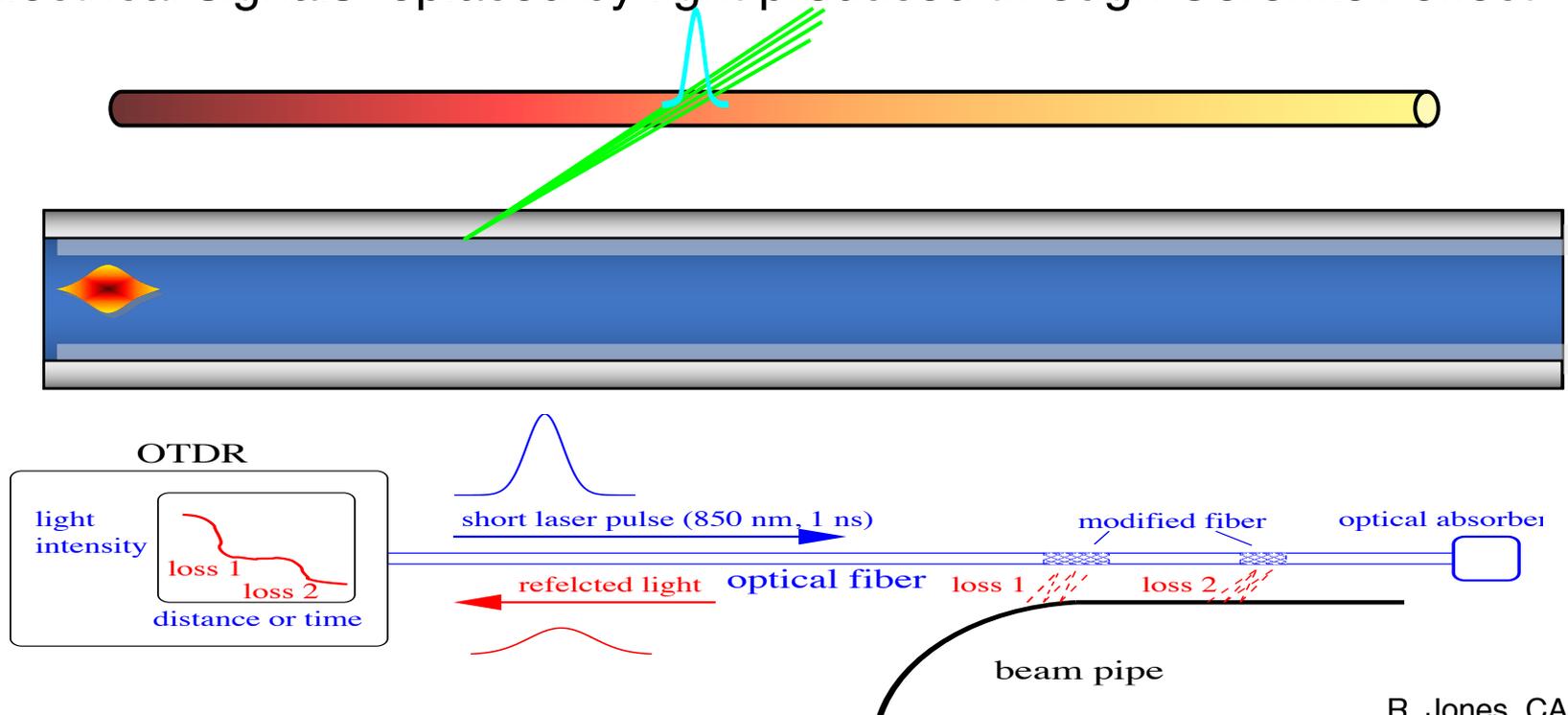
Beam Loss Monitors

Long ionization chamber (charge detection)

- Up to several km of gas filled hollow coaxial cables
- Position sensitivity achieved by comparing direct & reflected pulse
- SLAC – 8m position resolution (30ns) over 3.5km cable length

Fiber optic monitors

- Electrical signals replaced by light produced through Cerenkov effect

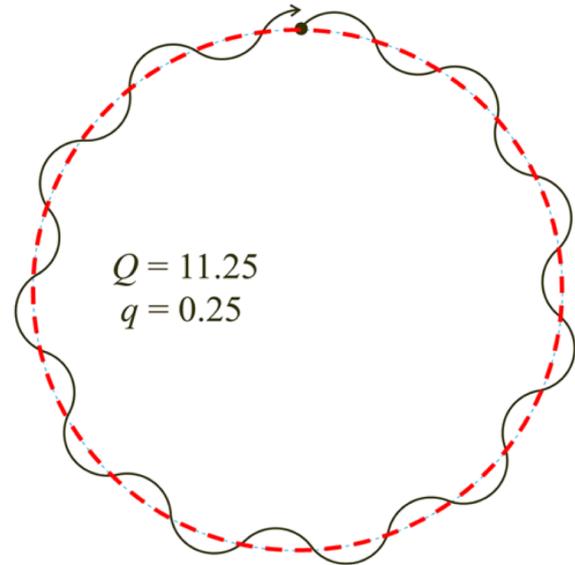


Tune, Chromaticity, Momentum

Tune

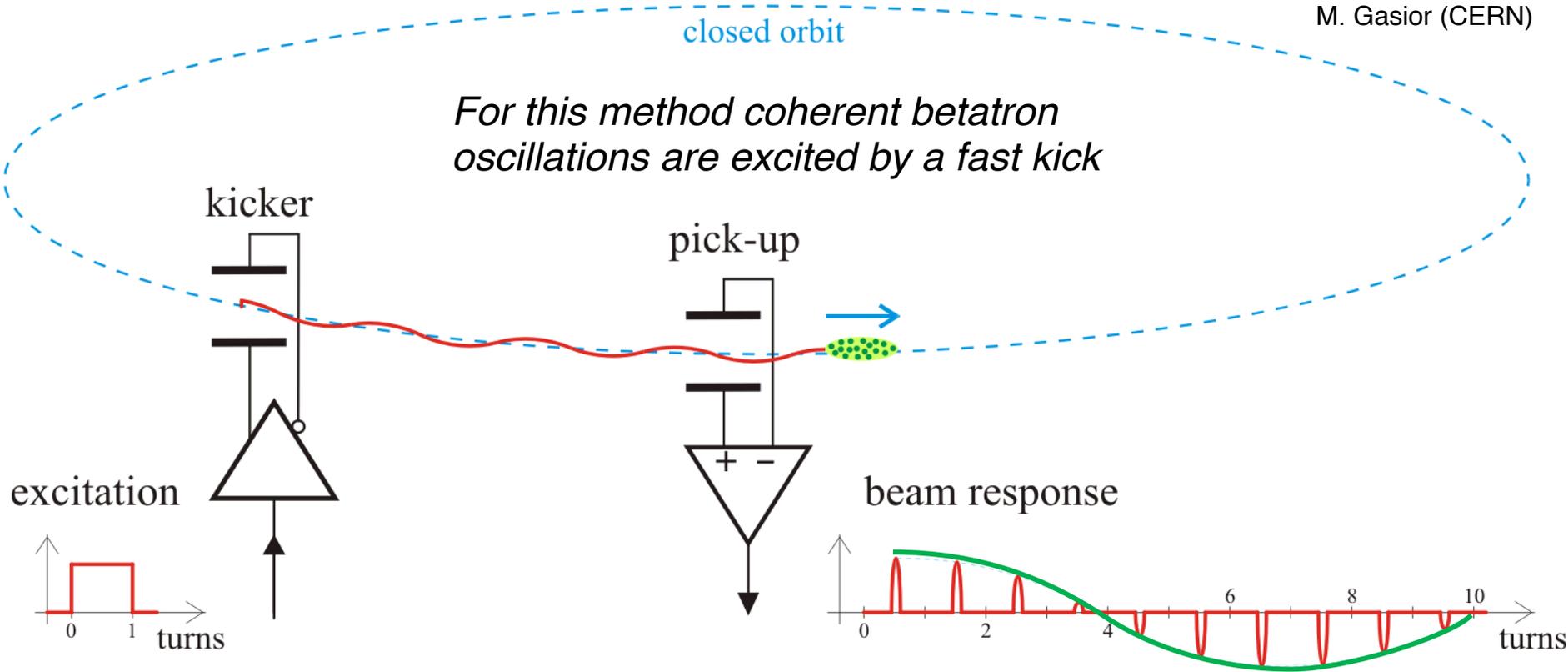
Characteristic Frequency of the Magnetic Lattice Given by the strength of the Quadrupole magnets

- Parameters
 - Q : Full betatron tune
 - n : Integer tune
 - q : Fractional tune ($Q=n+q$)
 - horizontal, vertical



Tune measurement – principle

M. Gasior (CERN)

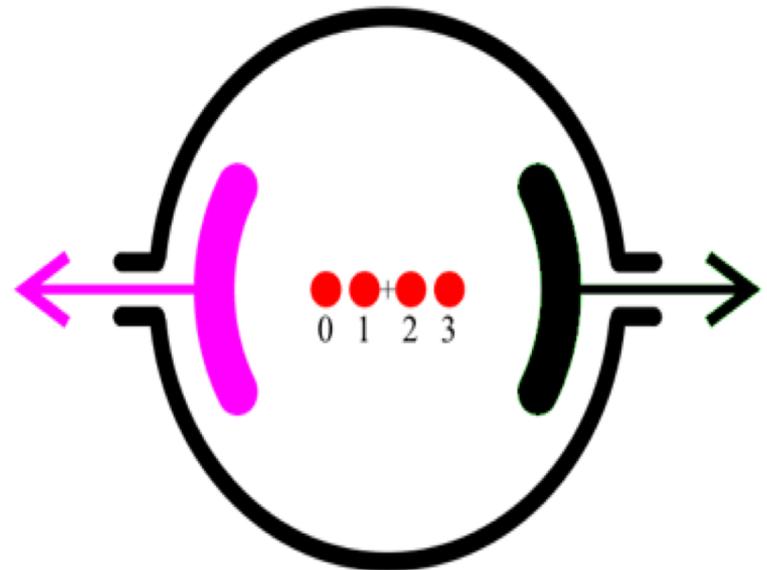
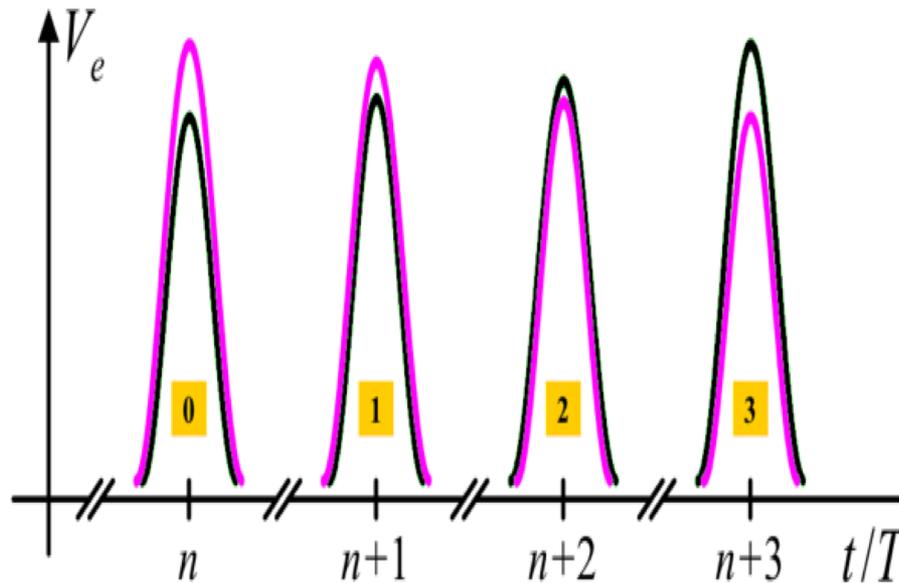


A **stimulus** is needed to globally excite the beam.

- Resulting betatron oscillations observed on a position pick-up
- Time domain signals usually converted to frequency domain
 - Displays which frequencies are present in the oscillations

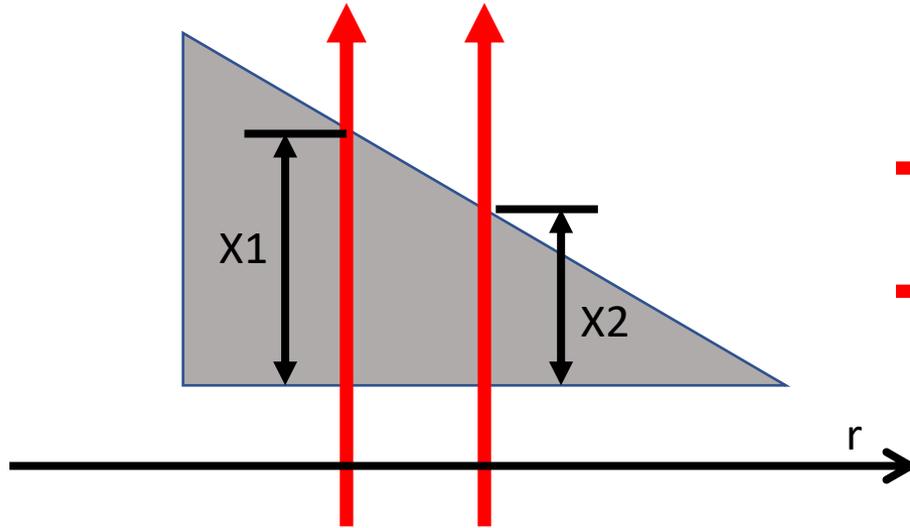
Tune measurement – principle

- Observable is typically turn-by-turn position from a BPM
- BPM electrode signal has temporal shape related to the temporal structure (intensity profile) of the passing beam

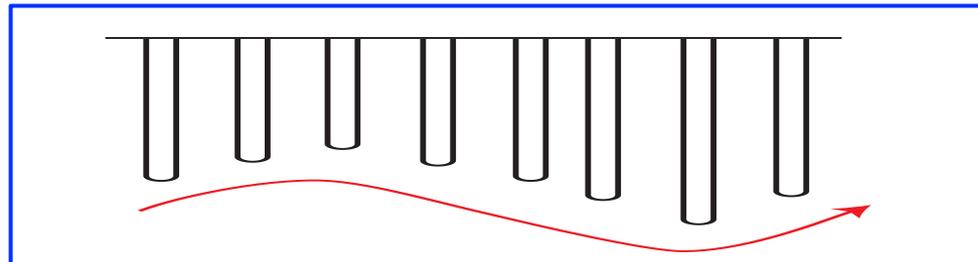
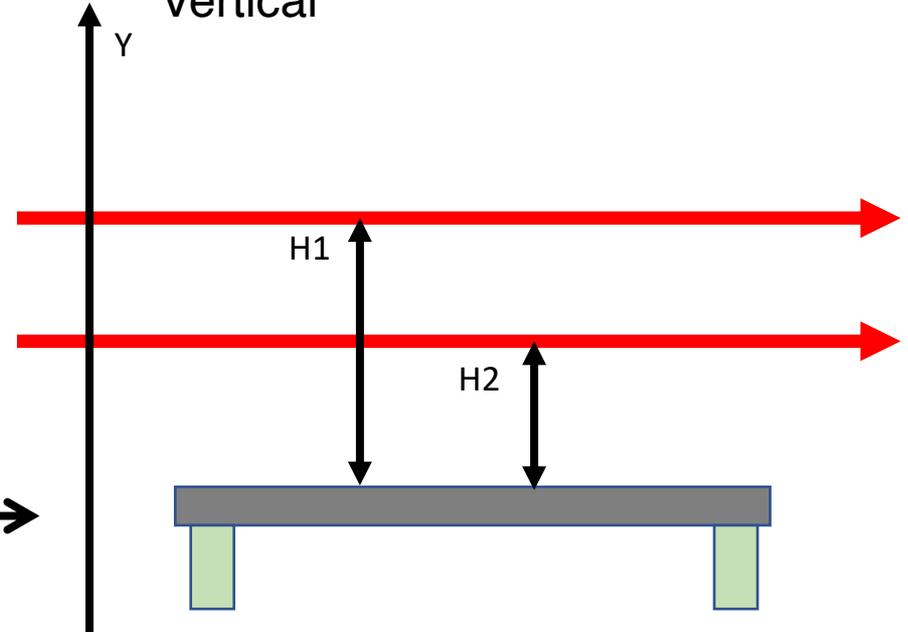


Tune measurement

Horizontal



Vertical



Induced voltage (pulse height) each turn depends on **path length of electrode** by the betatron oscillations.

Induced voltage (pulse height) each turn depends on **distance between beam-electrode** by the betatron oscillations.

Tune measurement by FFT analysis

Measured voltage from monitor

$$V_{\text{moni}} = \sum_m A \{1 + A_b \cos(2\pi f_b t + \theta)\} \cdot \delta\left(t - \frac{m}{f_{\text{rev}}}\right)$$

tune $\nu = \frac{f_b}{f_{\text{rev}}} = n + c$

$$V_{\text{moni}} = \sum_m A \{1 + A_b \cos(2\pi(n + c)f_{\text{rev}}t + \theta)\} \cdot \delta\left(t - \frac{m}{f_{\text{rev}}}\right)$$

$$= \sum_m A \{1 + A_b \cos(2\pi c f_{\text{rev}}t + \theta) \cos(2\pi n f_{\text{rev}}t)$$

$$- A_b \sin(2\pi c f_{\text{rev}}t + \theta) \sin(2\pi n f_{\text{rev}}t)\} \cdot \delta\left(t - \frac{m}{f_{\text{rev}}}\right)$$

$$= \sum_m A \{1 + A_b \cos(2\pi c f_{\text{rev}}t + \theta) \cos(2\pi n f_{\text{rev}}t)\} \cdot \delta\left(t - \frac{m}{f_{\text{rev}}}\right)$$

n : integer tune

c : fractional part of tune

f_{rev} : revolution frequency

f_{side} : sideband frequency

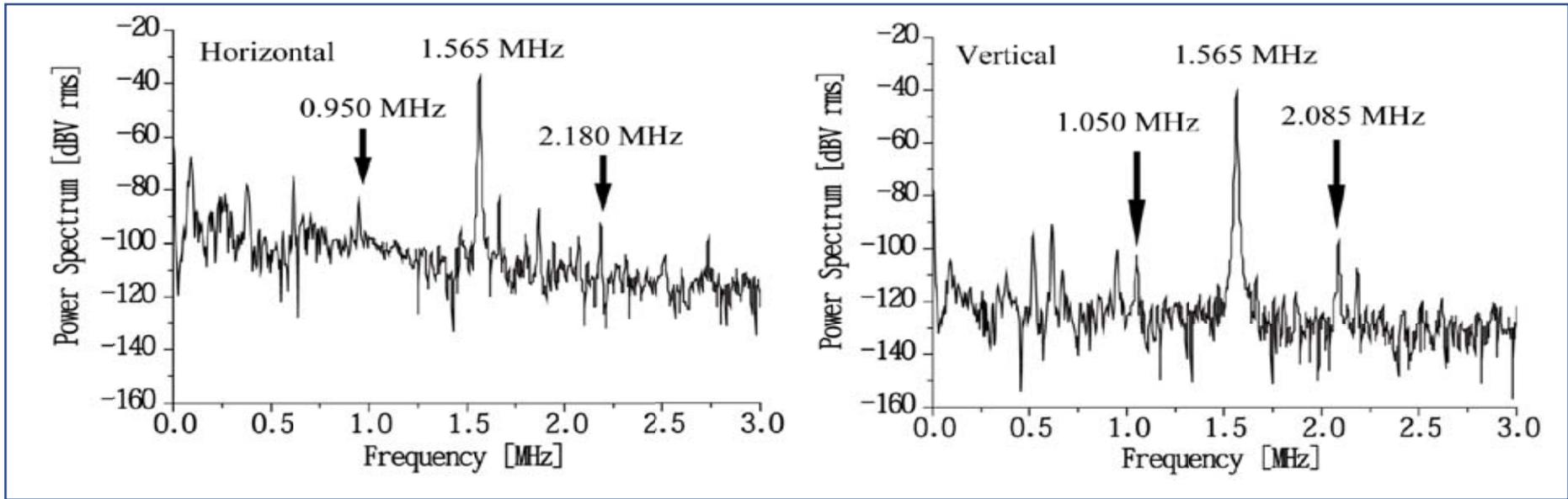
m : order of harmonic

$$V_{\text{moni}} = \sum_m A f_{\text{rev}} \left[\cos(2\pi m f_{\text{rev}}t) + \frac{A_b}{2} \cos\{2\pi(m + c)f_{\text{rev}}t + \theta\} + \frac{A_b}{2} \cos\{2\pi(m - c)f_{\text{rev}}t + \theta\} \right]$$

$$c = \frac{|f_{\text{side}} - m f_{\text{rev}}|}{m f_{\text{rev}}}$$

Tune measurement by FFT analysis (example)

example: Kyushu FFAG, 10MeV proton beam



$$\nu = \frac{f_b}{f_{rev}} = n + c$$

$$c = \frac{|f_{side} - m f_{rev}|}{m f_{rev}}$$

n : integer tune

c : fractional part of tune

f_{rev} : revolution frequency

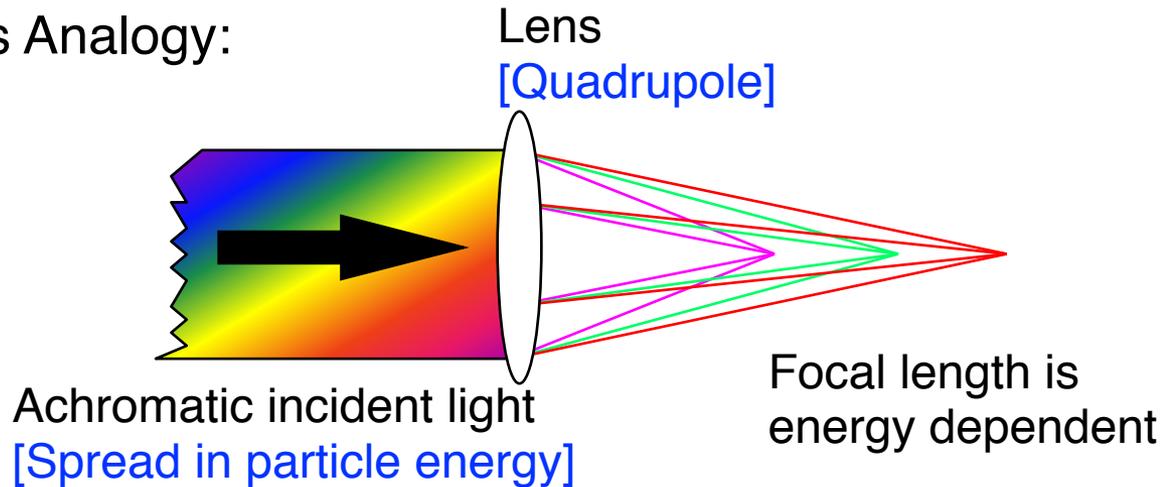
f_{side} : sideband frequency

m : order of harmonic

ν in holiz. & vert. --> "tune diagram"

Chromaticity

Optics Analogy:



Spread in the Machine Tune due to Particle Energy Spread
(Relative increase in tune for an off-momentum particle)

Chromaticity ξ $Q' = \xi Q$

tune change $\Delta Q = Q' \frac{\Delta p}{p}$ $\xi = \frac{\frac{\Delta Q}{Q}}{\frac{\Delta p}{p}}$ <-- momentum change

- **Measure tune for slightly different beam energies** (by varying RF frequency and keeping magnetic field constant and calculate the gradient).
- Correct with sextupole magnets.
- Chromaticity can be tracked continuously by combining RF modulation with PLL tune measurement.

Chromaticity Measurement

Many techniques available to measure chromaticity

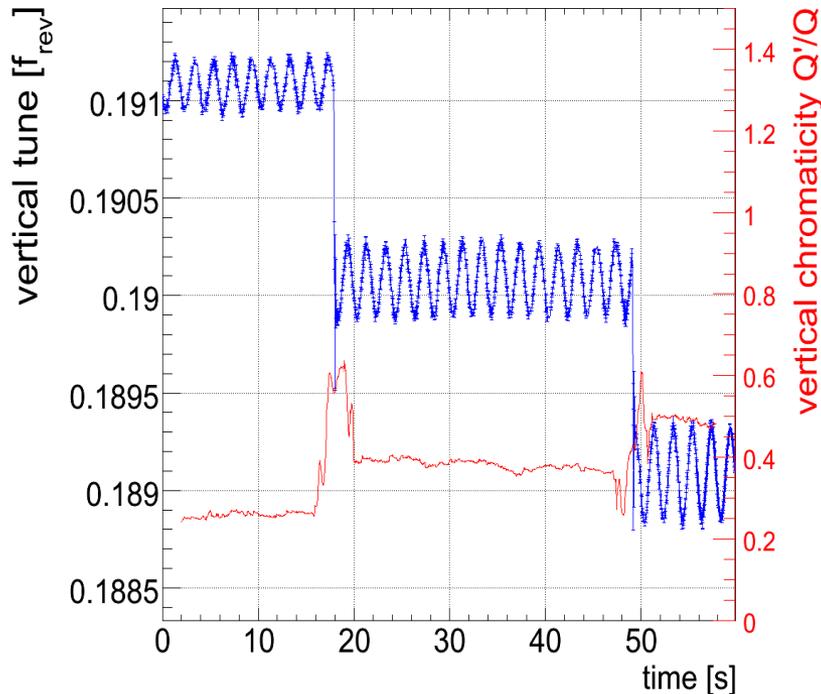
Tune change for different beam momenta	Standard method used on all machines. Can be combined with PLL tune tracking to give on-line measurement
Width of tune peak or damping time	Model dependent, non-linear effects, not compatible with active transverse damping
Amplitude ratio of synchrotron sidebands	Difficult to exploit in hadron machines with low synchrotron tune, Influence of collective effects
Width ratio of Schottky sidebands	Used on many machines & ideally suited to unbunched or ion beams. Measurement is typically very slow
Bunch spectrum variations during betatron oscillations	Difficult to disentangle effects from all other sources – e.g. bunch filling patterns, pick-up & electronics response
Head-tail phase advance	Good results on several machines but requires kick stimulus \Rightarrow emittance growth!

Chromaticity measurement in the LHC (Q' tracker)

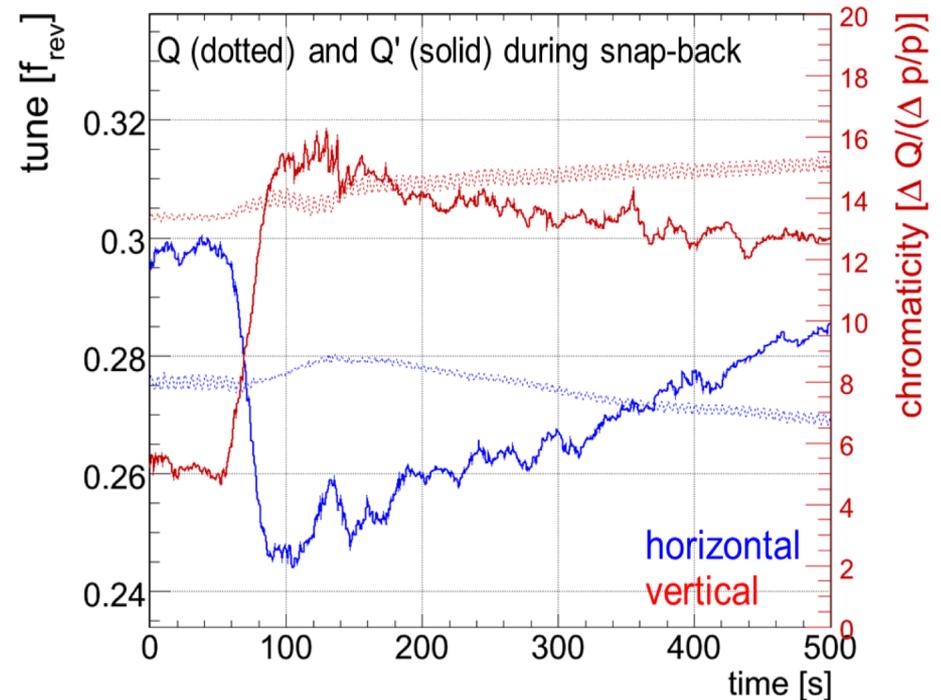
Modulates the RF frequency to give $\Delta p/p$ of 10^{-4} @ 2Hz

Measures the effect on the tune & demodulates the sinusoidal variation

Resolution of 1-2 units achieved with results fed-forward for next ramp



Test showing effect of RF modulation on tune in presence of chromaticity



Real-time tune & chromaticity measurement in the LHC during start of acceleration

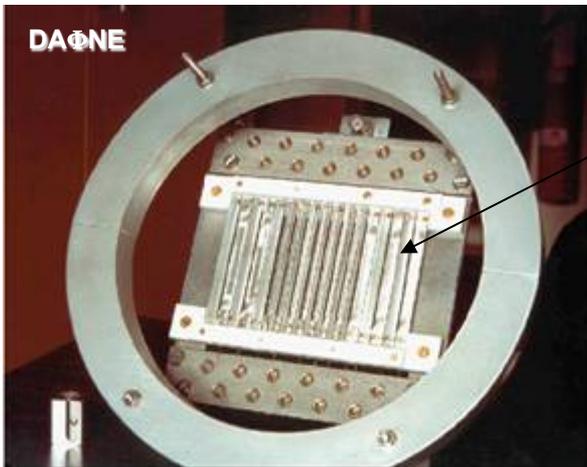
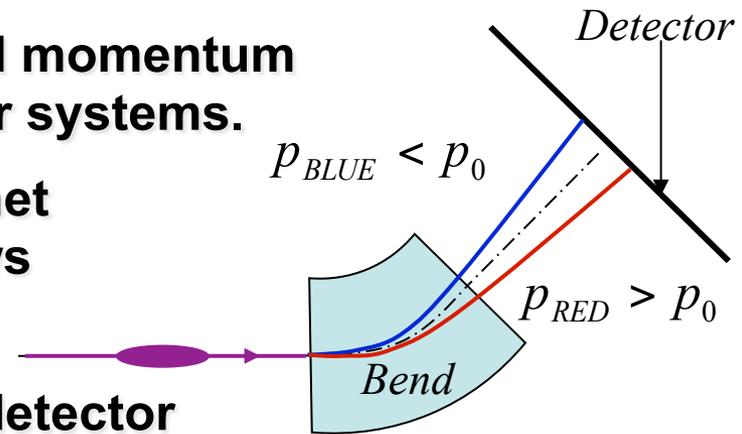
$$Q' = \frac{\Delta Q}{\Delta p/p}$$

ΔQ ← measured tune change
 $\Delta p/p$ ← RF induced momentum change

$$\xi = \frac{Q'}{Q}$$

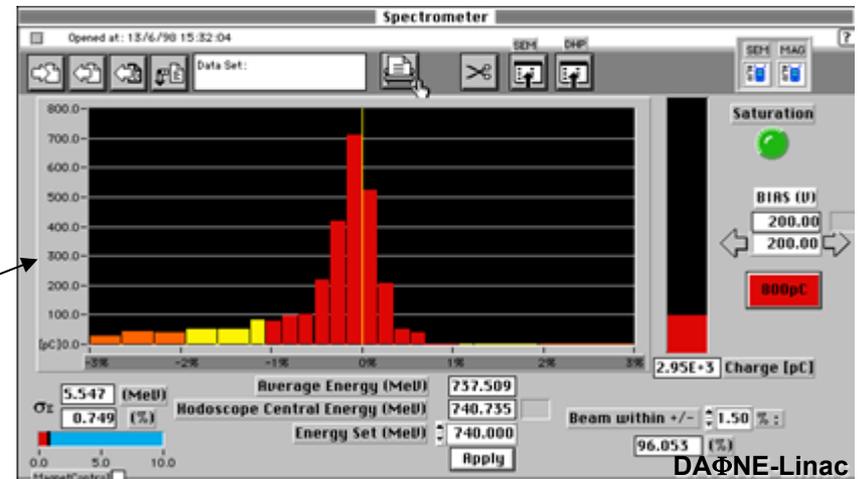
Momentum measurement

- In linacs and transferlines the momentum and momentum spread are mainly measured by spectrometer systems.
- The beam enters in the field of a dipole magnet where particles with different momenta follow different trajectories.
- The particle position is then measured on a detector downstream the magnet.



Secondary emission hodoscope

Spectrometer control window

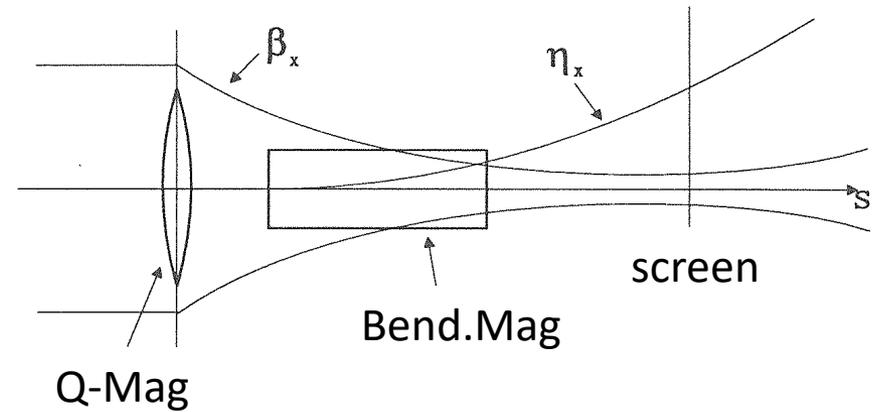


- The spectrometer resolution is limited by the intrinsic beam size at the detector plane and by field non-linearities.

Momentum measurement

Beam Size

$$\sigma_x = \sqrt{\beta_x \varepsilon_x + \left(\eta_x \frac{\sigma_p}{p} \right)^2}$$



β_x is minimized before passing through bending magnet using Q-magnet.
Beam size is measured at point where β_x is minimum.

$$\beta_x \varepsilon_x \ll \left(\eta_x \sigma_p / p \right)^2$$

$$\sigma_x \simeq \eta_x \frac{\sigma_p}{p}$$

beam size

dispersion

Overview of typical beam parameters and diagnostic instruments

Beam quantity		LINAC, transfer line	Synchrotron
current I	<i>general</i>	transformer (dc, pulsed) Faraday cup	transformer (dc)
	<i>special</i>	particle detector (Scint. IC, SEM)	normalized pick-up signal
position \bar{x}	<i>general</i>	pick-up	pick-up
	<i>special</i>	using profile measurement	cavity excitation (e^-)
profile x_{width}	<i>general</i>	SEM-grid, wire scanner viewing screen, OTR-screen	residual gas monitor synch. radiation (e^-) wire scanner
	<i>special</i>	grid with ampl. (MWPC)	
trans. emittance ϵ_{trans}	<i>general</i>	slit grid quadrupole scan	residual gas monitor wire scanner
	<i>special</i>	pepper-pot	transverse Schottky pick-up wire scanner
momentum p and $\Delta p/p$	<i>general</i>	pick-up (TOF) magn. spectrometer	pick-up
	<i>special</i>		Schottky noise pick-up
bunch width $\Delta\varphi$	<i>general</i>	pick-up	pick-up wall current monitor
	<i>special</i>	particle detector secondary electrons	streak camera (e^-)
long. emittance ϵ_{long}	<i>general</i>	magn. spectrometer buncher scan	
	<i>special</i>	TOF application	pick-up + tomography
tune, chromaticity Q, ξ	<i>general</i>	—	exciter + pick-up (BTF)
	<i>special</i>	—	transverse Schottky pick-up
beam loss r_{loss}	<i>general</i>	particle detector	
polarization P	<i>general</i>	particle detector	
	<i>special</i>	Compton scattering with laser	
luminosity \mathcal{L}	<i>general</i>	particle detector	